Quantum-Assisted Optical Inteferometry

Some forward-looking ideas and works in progress

In collaboration with: Andrei Nomerotski, Stephen Vintskevich, Anze Slosar, Michael Keach, Olli Saira, Jonathan Schiff, Alex Parsells, Tom Tsang (BNL)

https://www.quantastro.bnl.gov



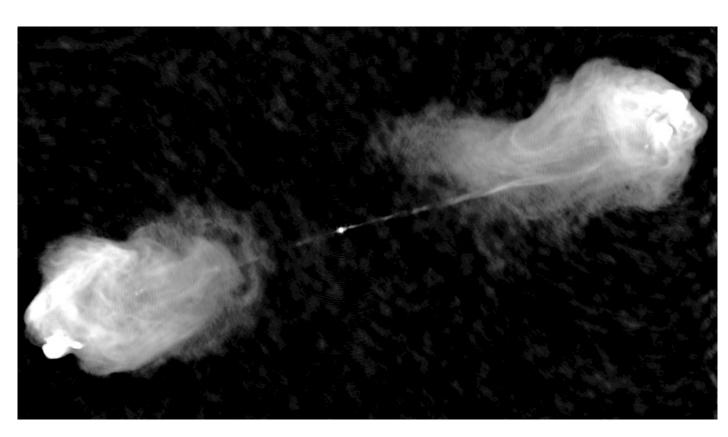
Paul Stankus, BNL Harvard Lukin Group Seminar 9 April 2021

 $\langle BNL|\hat{a}^{\dagger}|QIST\rangle$

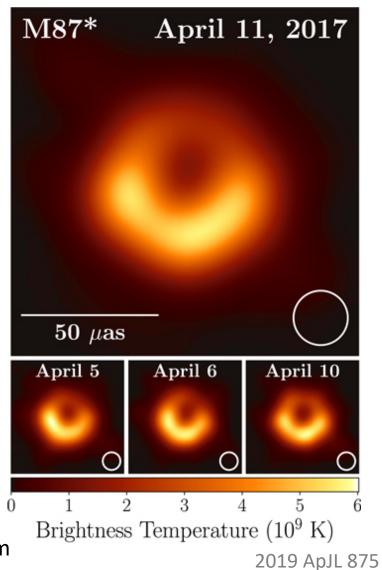
Agenda

- The glories of interferometry
- Single-photon methods (classical)
- Two-photon methods (quantum mechanical)
- Quantum assist; futuristic ideas
- New: two-photon interference for precision astrometry
- Astrophysical applications
- Experiments and detectors

Astronomy pictures of the day year decade

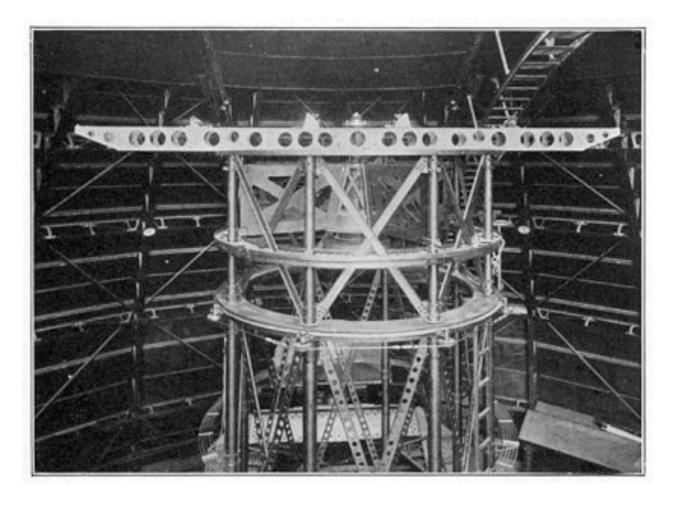


Radio source Cygnus A imaged at 6cm

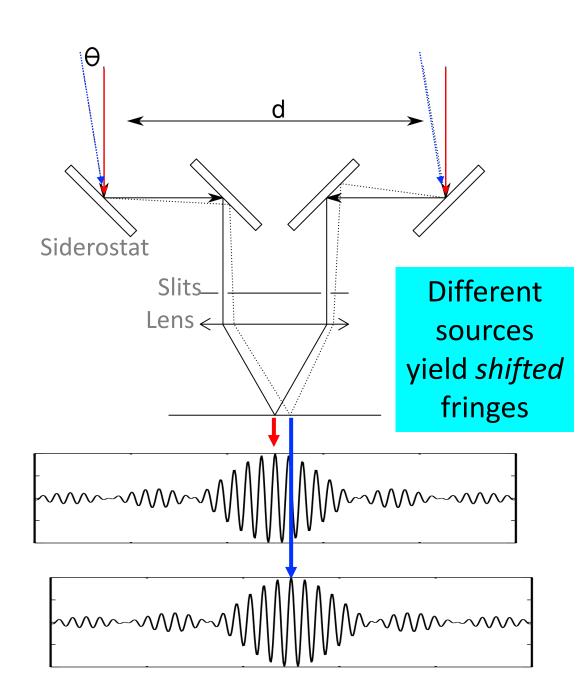


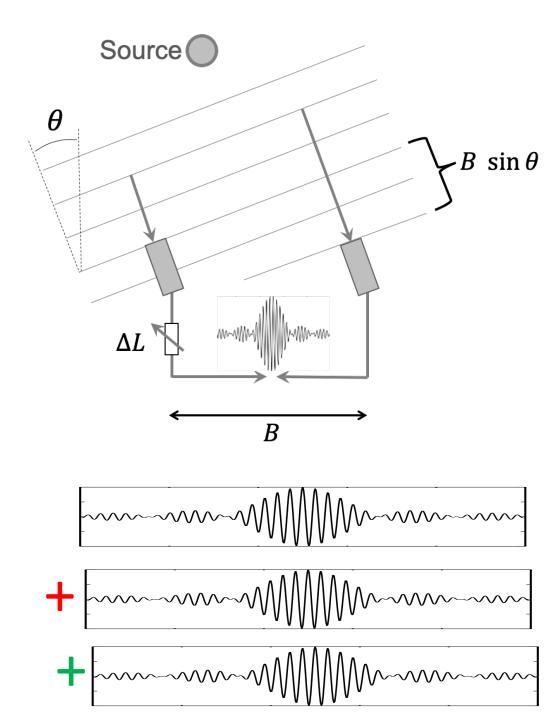
Single-photon techniques (classical)

In classical times



Michelson Stellar Interferometer at Mt. Wilson c. 1920, after original idea by Michelson & Fizeau c. 1890

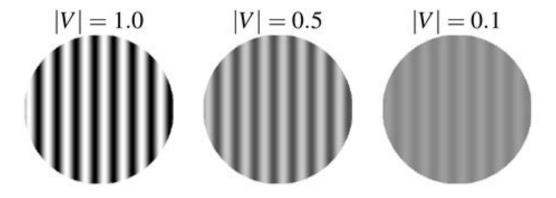




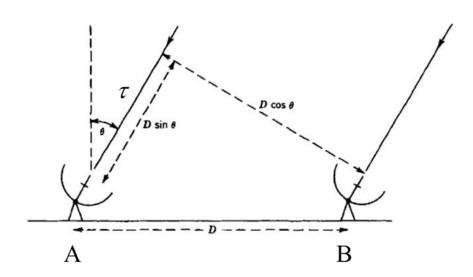
Each source i at sky position θ_i produces a fringe shifted by phase amount $\Delta \phi = 2\pi B \sin \theta_i/\lambda$

Intensity pattern is sum over all sources Fourier moment!

Fringe contrast(/visibility) measures <u>amplitude</u> of Fourier moment at wavenumber $k \approx 2\pi B/\lambda$

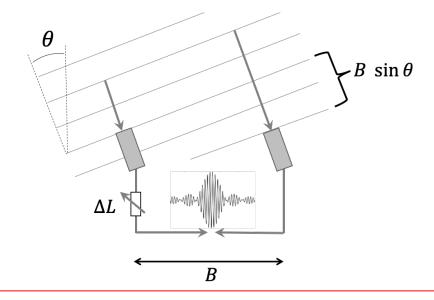


Radio $\bar{n} \gg 1$



Can literally record entire waveform, over some band, separately at each receiver station and interfere later offline

$_{\bar{n}}\ll _{1}\text{Optical}$



One photon at a time! Need to bring paths to common point in real time

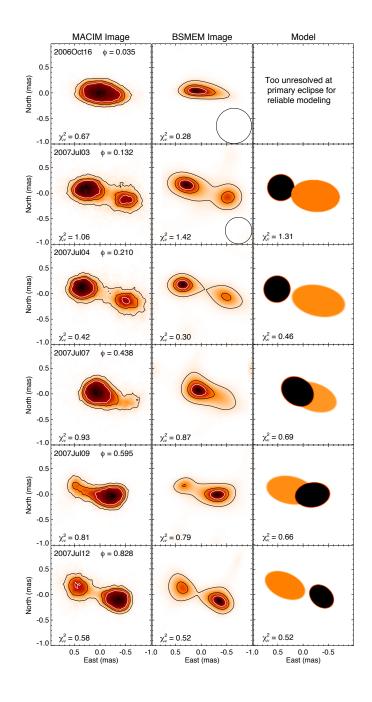
Need path length *compensated* to better than *c*/bandwidth

Need path length *stabilized* to better than λ

How cool is this?



CHARA Collaboration, "First Resolved Images of the Eclipsing and Interacting Binary β Lyrae"; arXiv:0808.0932, The Astrophysical Journal, 684: L95–L98, 2008 September 10



Classical summary

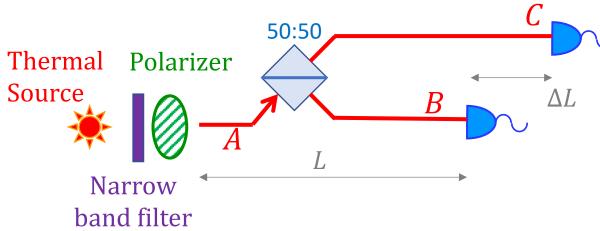
- EM waves interfere with themselves; single photons do same
- Interferometer sensitive to features on angular scale $\Delta\theta \sim \frac{\lambda}{B}$
- Drawbacks in *optical*:
 - Need live optical link between stations
 - Need path length control precision on order $\lambda^2/\Delta\lambda$
 - Atmospheric effects enter at O(1)
 - Need to control polarization during transport
 - Practical limit on baselines ~ 100m

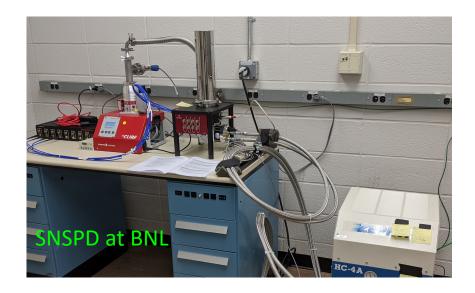
Two-photon techniques (quantum mechanical)

Prelude: Two-photon Intensity Interferometry

The curious HBT effect

"The birth of quantum optics"





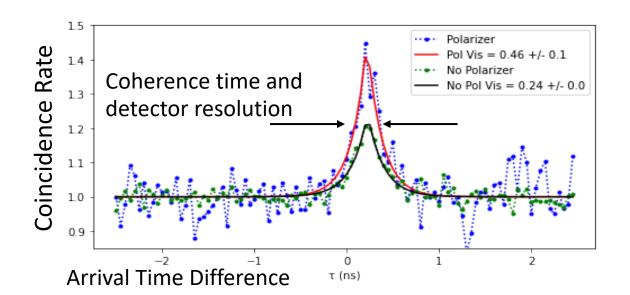
Glauber theory of photodetection, c. 1963

Rate^{BC}
$$(t_B, t_C) \propto \|\hat{a}_B(t_B) \hat{a}_C(t_C) |\Psi\rangle\|^2$$

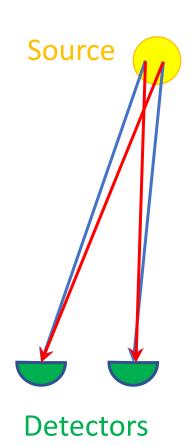
$$\propto \|\widehat{a}_A(t_B - L/v)\widehat{a}_A(t_C - (L + \Delta L)/v)\|\Psi\rangle\|^2$$

If
$$(t_B - L/v) = (t_C - (L + \Delta L)/v) = t_A$$

then Rate^{BC} $(t_B, t_C) \propto ||\hat{a}_A(t_A)^2|\Psi_{Th}\rangle||^2$
 $||\hat{a}_A(t_A)^2|\Psi_{Th}\rangle||^2 = 2||\hat{a}_A(t_A)\hat{a}_A(t_A')|\Psi_{Th}\rangle||^2$



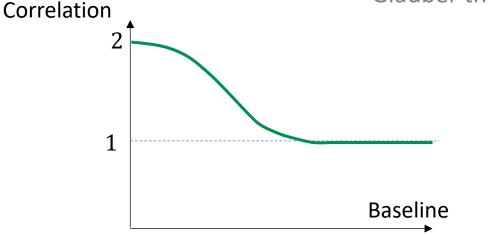
HBT and stellar sizes



In Hanbury Brown & Twiss (HBT) **intensity interferometry**, the observable is the *correlation* between photon detections at two separate detectors

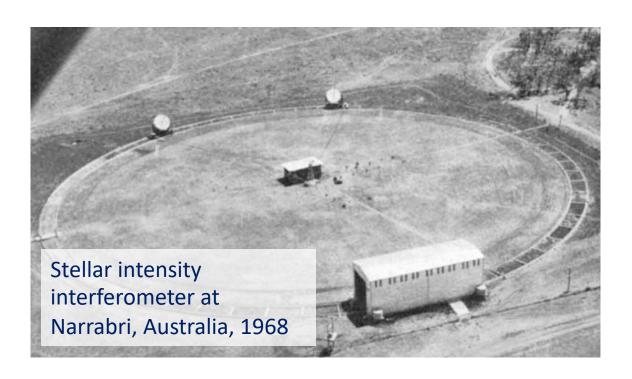
$$\frac{(Pairs)}{(Singles)(Singles)} = \frac{\left\|\hat{a}_{\overrightarrow{k1}}\hat{a}_{\overrightarrow{k2}}|\Psi\rangle\right\|^{2}}{\left\|\hat{a}_{\overrightarrow{k1}}|\Psi\rangle\right\|^{2}\left\|\hat{a}_{\overrightarrow{k2}}|\Psi\rangle\right\|^{2}} = \begin{cases} 1 & \overrightarrow{k1} \neq \overrightarrow{k2} \\ 2 & \overrightarrow{k1} = \overrightarrow{k2} \end{cases}$$

Glauber theory of photodetection, c. 1963



(It works for other bosons, too.)

High ride of HBT, 1956-1974 ...and beyond?



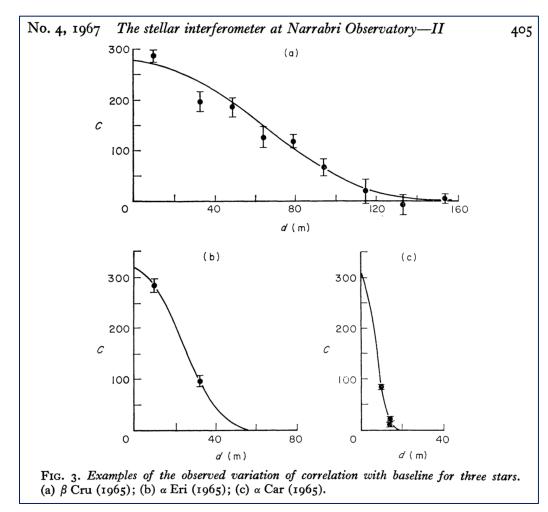
arXiv.org > astro-ph > arXiv:1810.08023

Astrophysics > Instrumentation and Methods for Astrophysics

Intensity Interferometry revival on the Côte d'Azur

Olivier Lai, William Guerin, Farrokh Vakili, Robin Kaiser, Jean Pierre Rivet, Mathilde Fouché, Guillaume Labeyrie, Etienne Samain, David Vernet

(Submitted on 18 Oct 2018)



Hanbury Brown, Davis, Allen, Rome; MNRAS 137, (1967) p393-417

HBT track record

Advantages:

- Separate stations with only classical connection
- Arbitrary baselines, set by desired angular scale
- No path-length corrections needed
- Immune to atmospheric effects (at leading order)

Drawbacks:

- Low rates! Need to see coincident photon pairs, only pairs with $\Delta \nu \ \Delta t < 1$ will show effect; but more & finer spectral bins will help
- Sensitive to square of image Fourier moment, washes out fine details
- Used (thus far) mainly for gross features of bright objects

Two-photon techniques (quantum mechanical)

New: Two-Photon Amplitude Interferometry

Improved single photon interference?

PRL 109, 070503 (2012)

PHYSICAL REVIEW LETTERS

week ending 17 AUGUST 2012

3

Longer-Baseline Telescopes Using Quantum Repeaters

Daniel Gottesman*

Perimeter Institute for Theoretical Physics, Waterloo, Ontario, Canada

Thomas Jennewein

Institute for Quantum Computing, University of Waterloo, Waterloo, Ontario, Canada

Sarah Croke

Perimeter Institute for Theoretical Physics, Waterloo, Ontario, Canada (Received 25 October 2011; revised manuscript received 22 May 2012; published 16 August 2012)

$$\Psi^{\text{Initial}} = \psi_1 \psi_2 = \frac{1}{2} (\hat{a}^{\dagger} + e^{i\delta_1} \hat{e}^{\dagger}) (\hat{b}^{\dagger} + e^{i\delta_2} \hat{f}^{\dagger})$$

Sky photon Ground photon

Beam
$$\hat{a}^\dagger \rightarrow (\hat{c}^\dagger + \hat{d}^\dagger)/\sqrt{2}$$
 $\hat{b}^\dagger \rightarrow (\hat{c}^\dagger - \hat{d}^\dagger)/\sqrt{2}$ Splitters $\hat{e}^\dagger \rightarrow (\hat{g}^\dagger + \hat{h}^\dagger)/\sqrt{2}$ $\hat{f}^\dagger \rightarrow (\hat{g}^\dagger - \hat{h}^\dagger)/\sqrt{2}$

$$\Psi^{\text{Output}} = (1/4)(\hat{c}^{\dagger}\hat{c}^{\dagger} - \hat{d}^{\dagger}\hat{d}^{\dagger} + e^{i(\delta_{1} + \delta_{2})}(\hat{g}^{\dagger}\hat{g}^{\dagger} - \hat{h}^{\dagger}\hat{h}^{\dagger}) + (e^{i\delta_{1}} + e^{i\delta_{2}})(\hat{c}^{\dagger}\hat{g}^{\dagger} - \hat{d}^{\dagger}\hat{h}^{\dagger}) + (e^{i\delta_{1}} - e^{i\delta_{2}})(\hat{c}^{\dagger}\hat{h}^{\dagger} + \hat{d}^{\dagger}\hat{g}^{\dagger}))$$

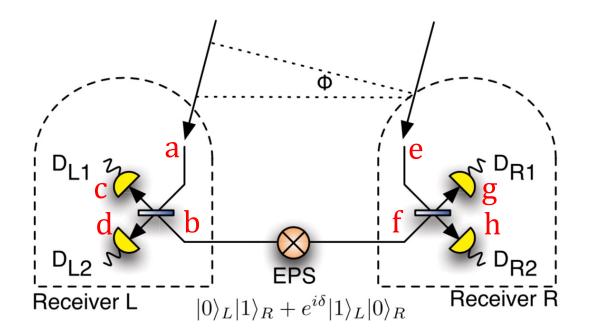
$$P(c^{2}) = P(d^{2}) = P(g^{2}) = P(h^{2}) = 1/8$$

$$P(cg) = P(dh) = (1/8)(1 + \cos(\delta_{1} - \delta_{2}))$$

$$P(ch) = P(dg) = (1/8)(1 - \cos(\delta_{1} - \delta_{2}))$$

Two-photon amplitude interferometry

$$\frac{N(cg) + N(dh) - \left(N(ch) + N(dg)\right)}{N(cg) + N(dh) + N(ch) + N(dg)}$$



New visibility observable:

$$\frac{N(cg) + N(dh) - \left(N(ch) + N(dg)\right)}{N(cg) + N(dh) + N(ch) + N(dg)}$$

$$= \cos(\delta_1 - \delta_2)$$

$$= \cos\left(\frac{2\pi \sin\theta \, b}{\lambda} - \delta_{Ground}\right)$$

- Same measurement as single-photon interferometry, if ground photons are available
- Can be interpreted as quantum teleportation of sky photon from one station to the other

Let slip the quantum technology!

PHYSICAL REVIEW LETTERS 123, 070504 (2019)

Optical Interferometry with Quantum Networks

E. T. Khabiboulline, ^{1,*} J. Borregaard, ^{1,2} K. De Greve, ¹ and M. D. Lukin ¹ Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA ² QMATH, Department of Mathematical Sciences, University of Copenhagen, 2100 Copenhagen Ø, Denmark

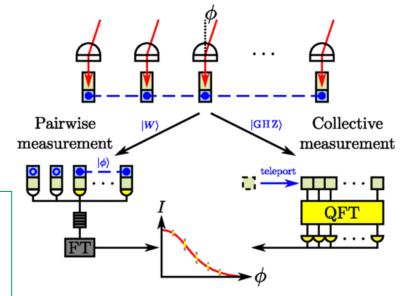
(Received 17 September 2018; published 15 August 2019)

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Idea: Efficient time-bin encoding of photon arrivals

Idea: Use quantum Fourier transform (QFT) to directly invert pattern from array

Idea: Capture and store sky photons in quantum memories, then teleport and measure as needed

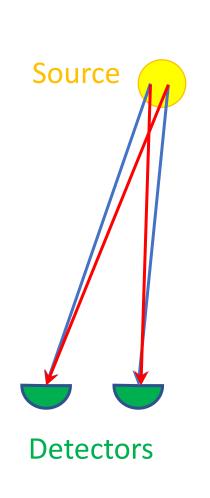


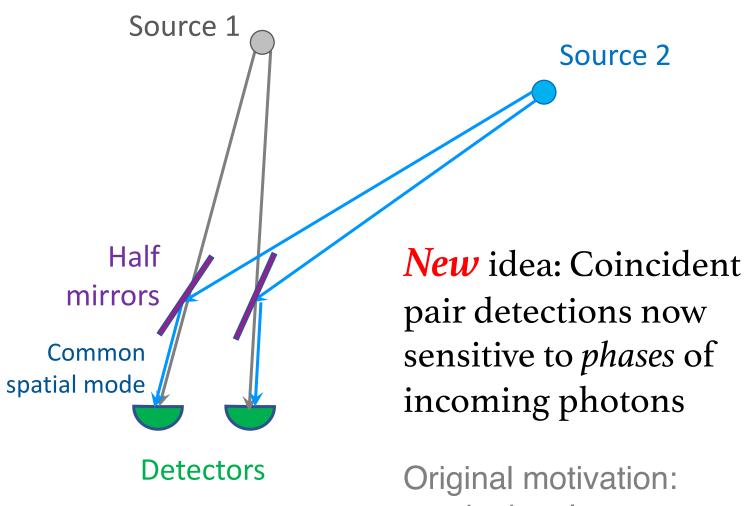
Two-photon spin-off technique

New: Two-Photon Amplitude Interferometry for *Astrometry**

* Astrometry = measurement of *positions* of objects on the sky

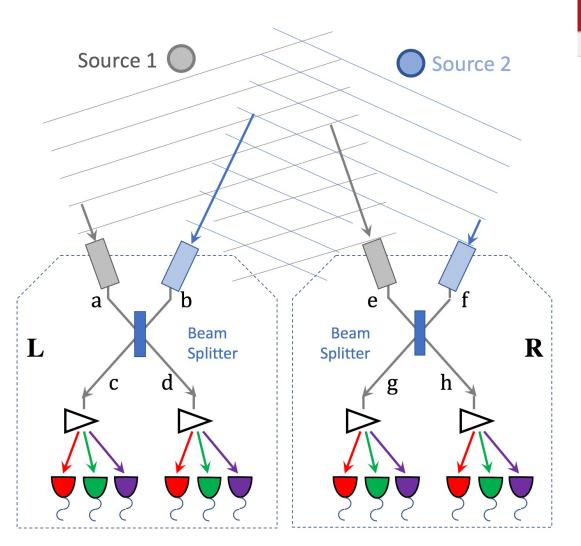
HBT with two sources?





gravitational waves

Idea: two photons from two sky sources



arXiv.org > astro-ph > arXiv:2010.09100

Astrophysics > Instrumentation and Methods for Astrophysics

[Submitted on 18 Oct 2020 (v1), last revised 4 Nov 2020 (this version, v2)]

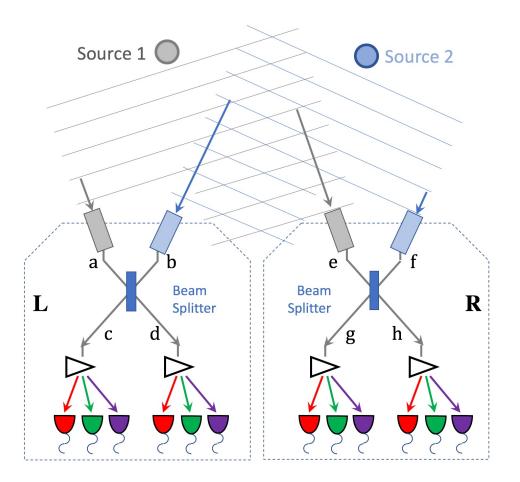
Two-photon amplitude interferometry for precision astrometry

Paul Stankus, Andrei Nomerotski, Anže Slosar, Stephen Vintskevich

Topology is equivalent to GJC(2012) but now with both photons from the sky, and from different objects

Sensitive to *difference* in path length differences opening angle!

Does *not* require live optical link between stations; can use arbitrary baseline



Observable is the number/rate of coincidences $xy = \{cg,dh\}$ or $\{ch,dg\}$ at different stations.

(Can do many spectral bins in parallel.)

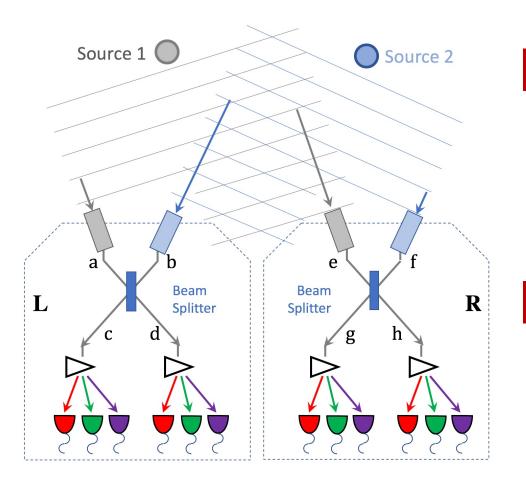
Quantum mechanics (Fock state) version; quickie:

$$\langle N(xy)\rangle = \frac{k(S_1 + S_2)^2}{8} \left[1 \pm V_{2PS} \cos \left[\frac{2\pi B}{\lambda} (\sin \theta_1 - \sin \theta_2) + \frac{2\pi \Delta L}{\lambda} \right] \right]$$

Quantum field theory version; full:

$$N_{c}(xy) = \eta_{1}\eta_{2}A^{2} \int_{0}^{T_{r}} P_{L,R,\tau}^{\text{two photons}} d\tau =$$

$$A^{2}\eta_{1}\eta_{2}T_{r} \left[(I_{1} + I_{2})^{2} + I_{1}^{2} \frac{\tau_{c}g_{11}}{T_{r}} + I_{2}^{2} \frac{\tau_{c}g_{22}}{T_{r}} \pm 2I_{1}I_{2} \frac{\tau_{c}g_{12}}{T_{r}} \cos \left(\frac{\omega_{0}B(\sin\theta_{1} - \sin\theta_{2})}{c} + \frac{\omega_{0}\Delta L}{c} \right) \right]$$



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Quantum field theory version; full:

Base combinatoric pair rate

$$\begin{split} N_c(xy) &= \eta_1 \eta_2 A^2 \int_0^{T_r} P_{L,R,\tau}^{\text{two photons}} d\tau = \\ A^2 \eta_1 \eta_2 T_r \left[(I_1 + I_2)^2 + I_1^2 \frac{\tau_c g_{11}}{T_r} + I_2^2 \frac{\tau_c g_{22}}{T_r} \pm \\ 2I_1 I_2 \frac{\tau_c g_{12}}{T_r} \cos \left(\frac{\omega_0 B(\sin \theta_1 - \sin \theta_2)}{c} + \frac{\omega_0 \Delta L}{c} \right) \right] & \text{Oscillatory term, fringe passing} \end{split}$$

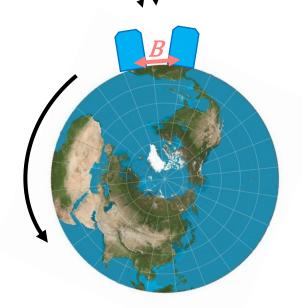
Idea: Earth rotation fringe scan

$$\langle N(xy)\rangle = \frac{k(S_1 + S_2)^2}{8} \left[1 \pm V_{2PS} \cos \left[\frac{2\pi B}{\lambda} (\sin \theta_1 - \sin \theta_2) + \frac{2\pi \Delta L}{\lambda} \right] \right]$$



This will evolve as the Earth rotates

$$\langle N_{xy} \rangle (t) = \bar{N}_{xy} \left[1 \pm V \cos \left(\omega_f t + \Phi \right) \right]$$
 Coincidence rates oscillate



$$\omega_f = \frac{2\pi B\Omega_{\oplus}\sin\theta_0}{\lambda}\Delta\theta$$

Fringe oscillation rate is a direct measure of sources' opening angle!

Can measure with high precision

World-competitive precision

$$\sigma \left[\Delta \theta \right] = \sqrt{\frac{6}{\pi^2 \kappa}} \, \frac{1}{V} \, \frac{\lambda}{B} \, \frac{1}{T \Omega_{\oplus} \sin \theta_0} \, \frac{1}{\sqrt{\bar{n}T}}$$

 \overline{n} = average pair rate

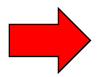
T = total observation time

A modest experiment:

- Bright stars, mag 2
- 1 m² collecting area
- 10⁴ seconds observation
- 0.15 nsec time resolution
- 10⁴ spectral channels

Idea: Dynamic Astrometry

Track day-over-day changes in $\Delta \theta$ to observe parallax, proper motion, orbital motion, gravitational lensing



$$\sigma[\Delta \theta] \sim 10 \mu {
m as} \ (\sim 10^{\text{-}11} \, {
m rad})$$

1 mas HIPPARCOS (1989-1993) 7 μ as GAIA (2013-)

Astrophysics topics in dynamic astrometry

- Parallax: improved distance ladder
- Proper motions: local dark matter patterns
- Microlensing, see motions and shape changes
- Gravitational waves at mid-frequency
- Quantum applications, e.g. quantum key distribution

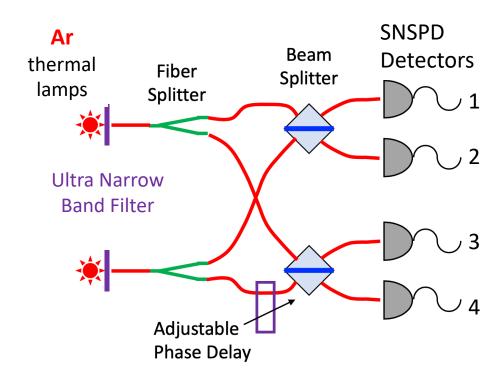
Further ideas are encouraged!

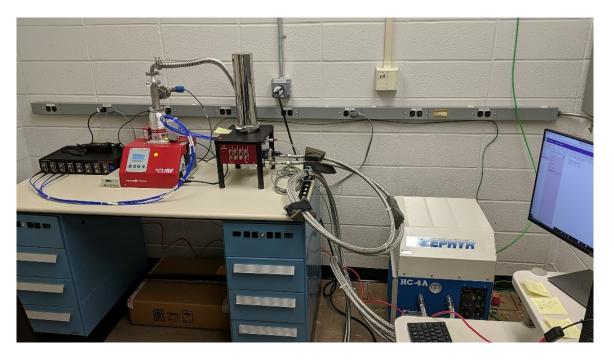
Experiments and Detectors

What are we going to need?

Experiments in progress

Supported at BNL by DOE HEP QuantISED grant 2020-21



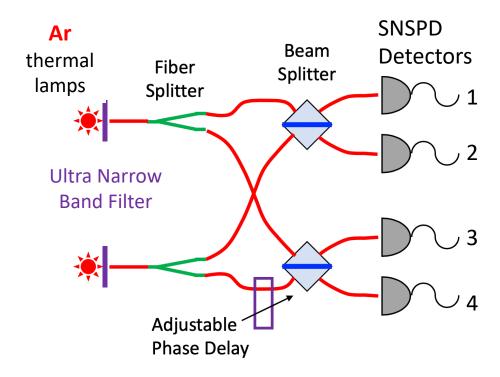


Superconducting Nanowire Single Photon Detector (SNSPD) at BNL

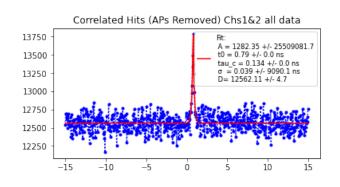
Four channels at ~795nm

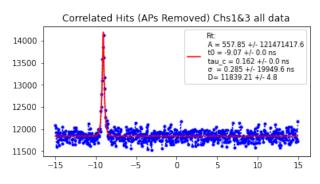
Experiments in progress

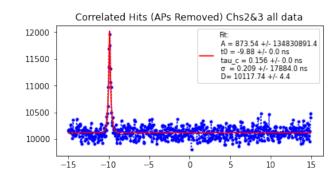
Supported at BNL by DOE HEP QuantISED grant 2020-21

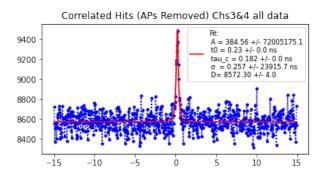


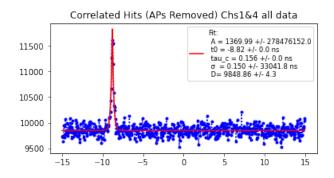
Check: We can see HBT coincidence enhancement peak in all channel combinations

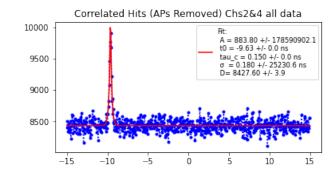






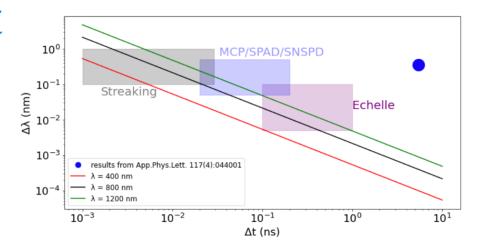


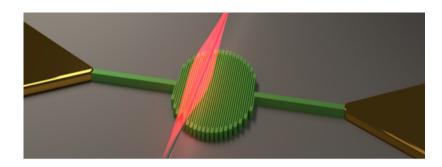


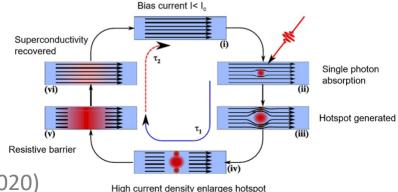


Future detector requirement

- Two essential figures of merit:
 - Number of detectors/spectroscopic channels (more pairs)
 - Detector time resolution (wider spectroscopic bins, more pairs per detector)
- Fast pixel array (Timepix) + dispersive spectrograph (Echele?)
- Very fast single photon detectors improved SNSPD? Timing, QE, many channels







Intensified camera is single photon sensitive

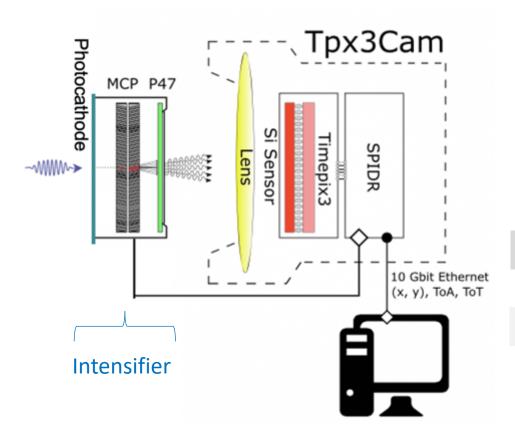
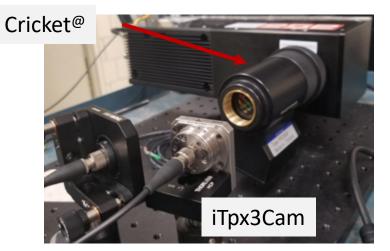




Image intensifier (Photonis PP0360EG)

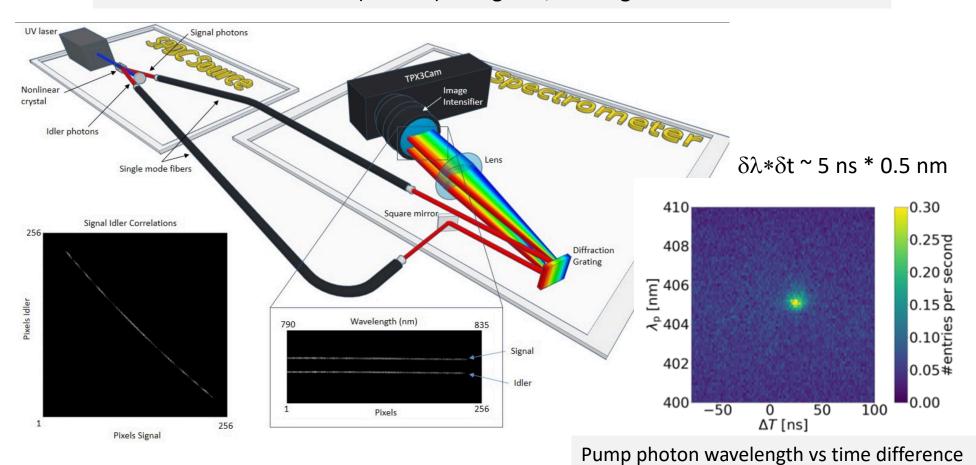


Quantum efficiency ~ 30%

A.Nomerotski, Imaging and time stamping of photons with nanosecond resolution in Timepix based optical cameras, NIM **A** 937 (2019) 26

Spectroscopic binning already demonstrated

In collaboration with NRC (Ottawa) D.England, Y.Zhang et al

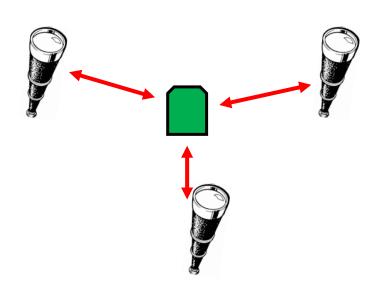


Y Zhang, D England, A Nomerotski, P Svihra et al, Multidimensional quantum-enhanced target detection via spectrotemporal-correlation measurements, Physical Review A 101 (5), 053808

P Svihra et al, Multivariate Discrimination in Quantum Target Detection, Appl. Phys. Lett. **117**, 044001 (2020)

Just the beginning! A broad future program

- Observations with >2 receivers and >2 objects; phase closure?
- More complicated quantum states (GHZ, etc.)
- New kinds of entanglement distribution (polarization qubits, e.g.)
- Involvement of quantum memories to enhance pair rates; local expertise (SBU) with ⁸⁷Rb vapor room-temp QM's
- Atmospheric effect compensation
- On-sky experiments possible soon!



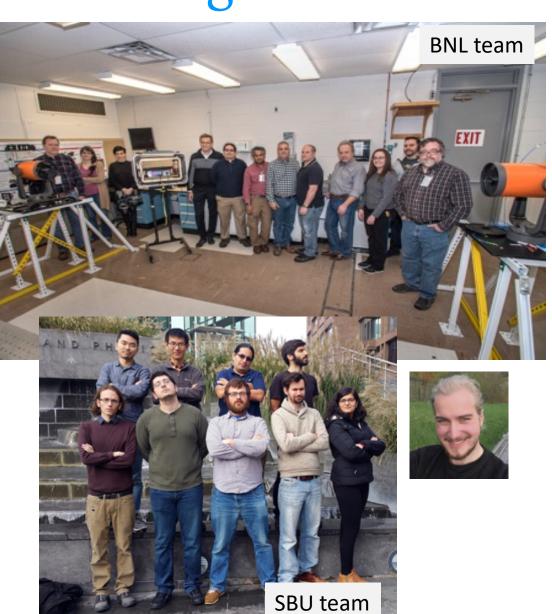
Points to take home

- Classical, single-photon interferometry reaches much higher resolutions, order milli-arcsec, than single telescopes; but practical issues limit maximum baselines
- Two-photon interferometry can permit independent stations over longer baselines; historical HBT is one example
- Two-photon techniques are in general quantum mechanical; new ideas suggest quantum technology can enhance interferometry
- One specific two-photon technique addresses dynamic astrometry, which will have interesting astrophysics applications
- There is a potentially broad program in quantum-assisted optical interferometry ahead

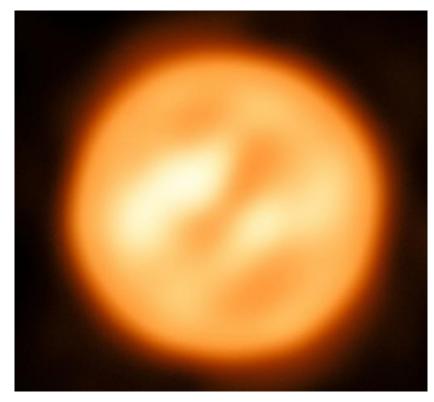
Acknowledgements

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Dimitros Katramatos
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Gabriella Carini
David Asner
Anand Kandasamy
Michael Keach
Steven Paci

Jingming Long
Martin van Beuzekom
Bram Bouwens
Erik Maddox
Jord Prangsma
Duncan England
Yingwen Zhang
Boris Blinov
Mila Zhukas
Maverick Millican
Peter Svihra



Backups



Dynamic convection on Antares (VLTI, ESO)

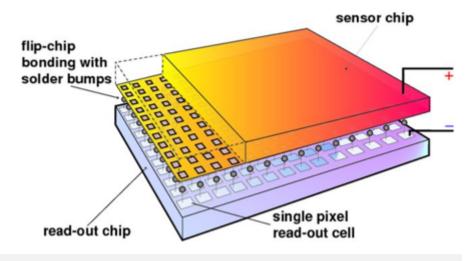
Each fringe observation measures amplitude and phase of Fourier moment along baseline vector at specific wavenumber.

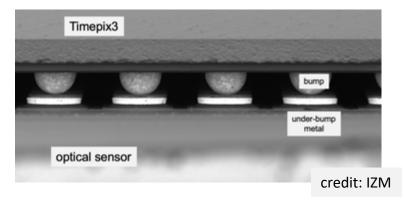
Repeat for many different baselines/wavenumbers and invert to reconstruct original image. (Note Earth rotation synthesis)

Measurement at baseline *B* sensitive to source features with angular size $\Delta\theta \sim \lambda/B$

Hybrid pixel detectors

Have roots in R&D for LEP/LHC vertex detectors





Lukas Tlustos and Erik H. M. Heijne, Performance and limitations of high granularity single photon processing X-ray imaging detectors, in CERN proceedings (2005)

- Decouple readout chip and sensor
- Optimize technologies for chip and sensor separately

Use different sensors with same readout, versatile approach for x-rays (Si, CZT)

→ we will use OPTICAL sensors

Timepix3 Camera -> Tpx3Cam

Camera = sensor + ASIC + readout

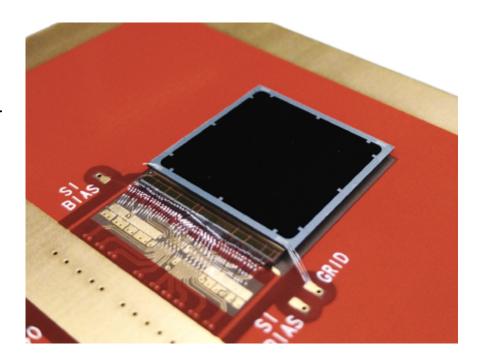
Optical sensor with high QE developed at BNL

Sensor is bump-bonded to chip Timepix3

Timepix3 ASIC:

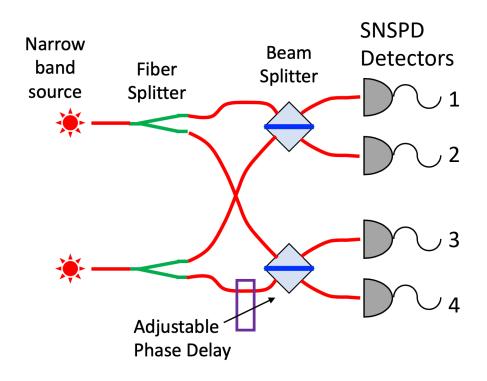
256 x 256 array, 55 x 55 micron pixel

- 1.56 ns timing resolution
- data-driven readout, 80 Mpix/sec, no deadtime



M. Fisher-Levine, A. Nomerotski, Timepixcam: a fast optical imager with time-stamping, Journal of Instrumentation 11 (03) (2016) C03016.

Pre-preliminary



(Pre-)Preliminary observation of anti-correlation between 1&3+2&4 pairs against 1&4+2&3 pairs, with random length/phase changes

