

Quantum-Assisted Optical Inteferometry

Some forward-looking ideas and works in progress

In collaboration with: Andrei Nomerotski, Stephen Vintskevich,
Anze Slosar, Michael Keach, Olli Saira, Jonathan Schiff, Alex
Parsells, Tom Tsang (BNL)

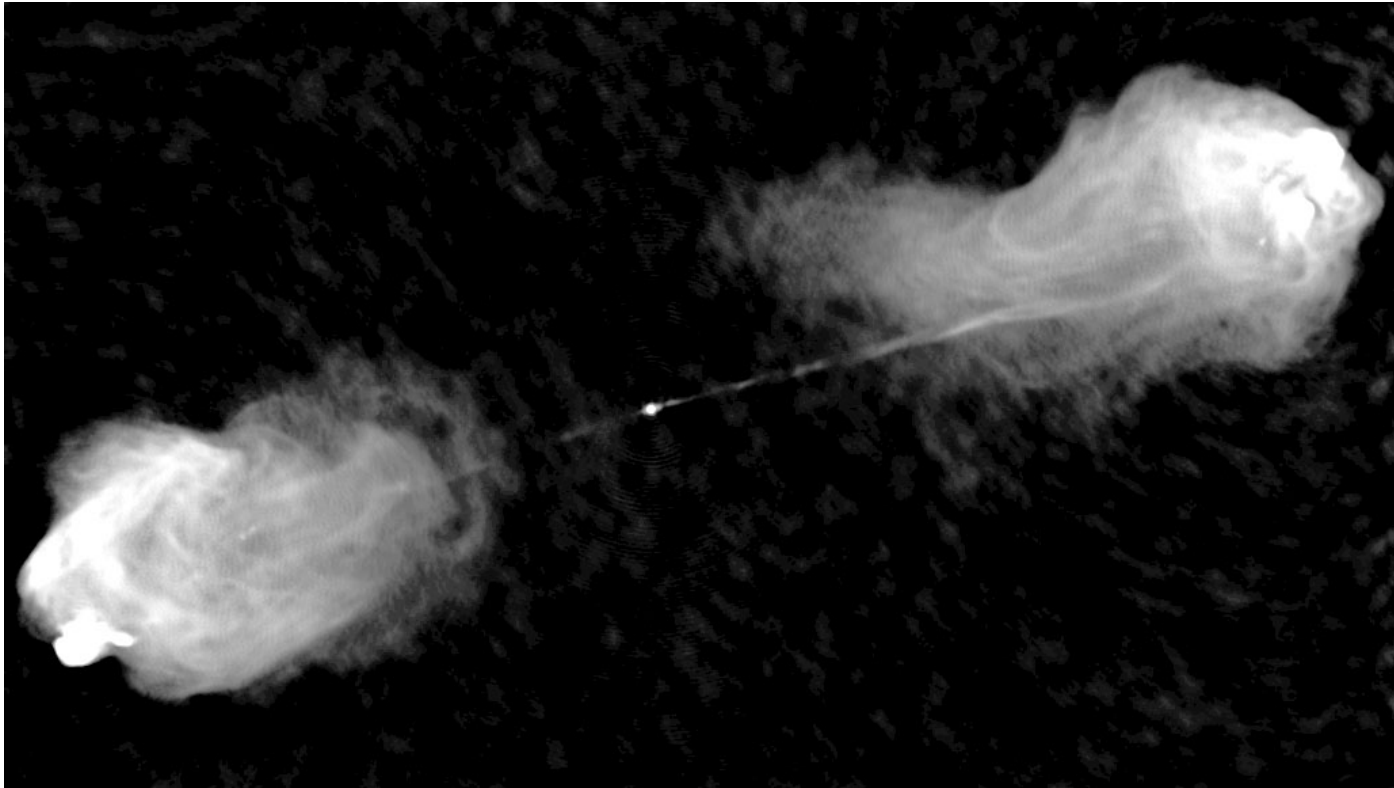
<https://www.quantastro.bnl.gov>

Paul Stankus, BNL
Caltech INQNET Seminar
1 March 2021

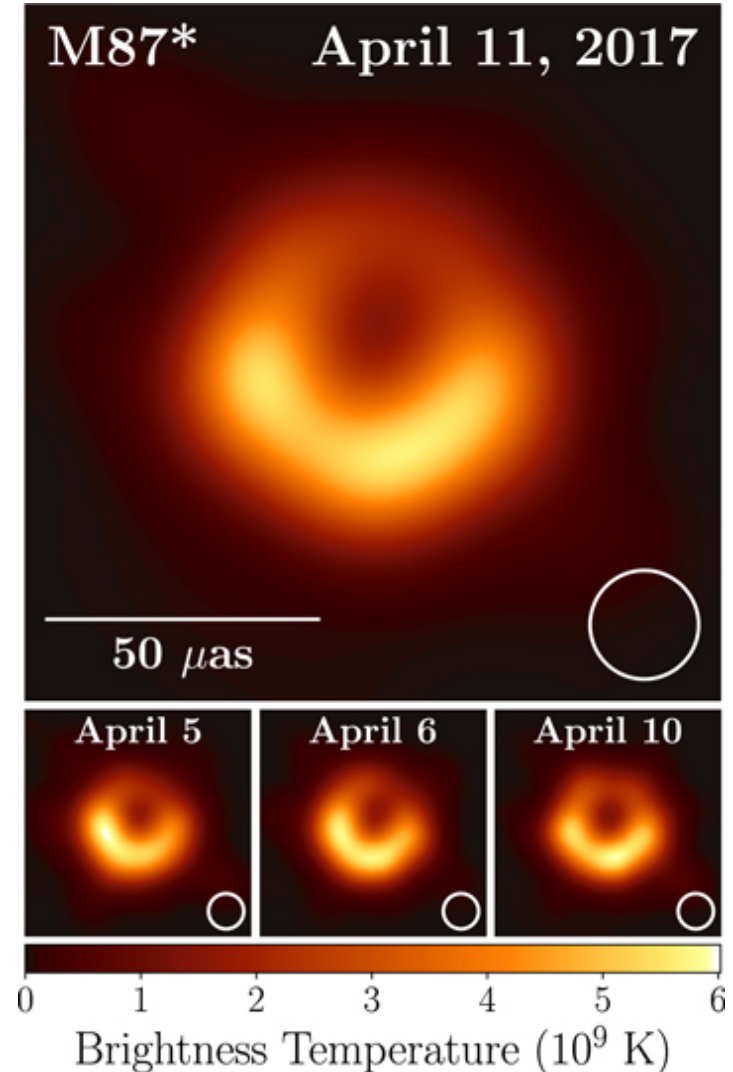
Agenda

- The glories of interferometry
- Single-photon methods (classical)
- Two-photon methods (quantum mechanical)
- Quantum assist; futuristic ideas
- **New:** two-photon interference for precision astrometry
- Astrophysical applications
- Experiments in progress

Astronomy pictures of the ~~day year~~ decade



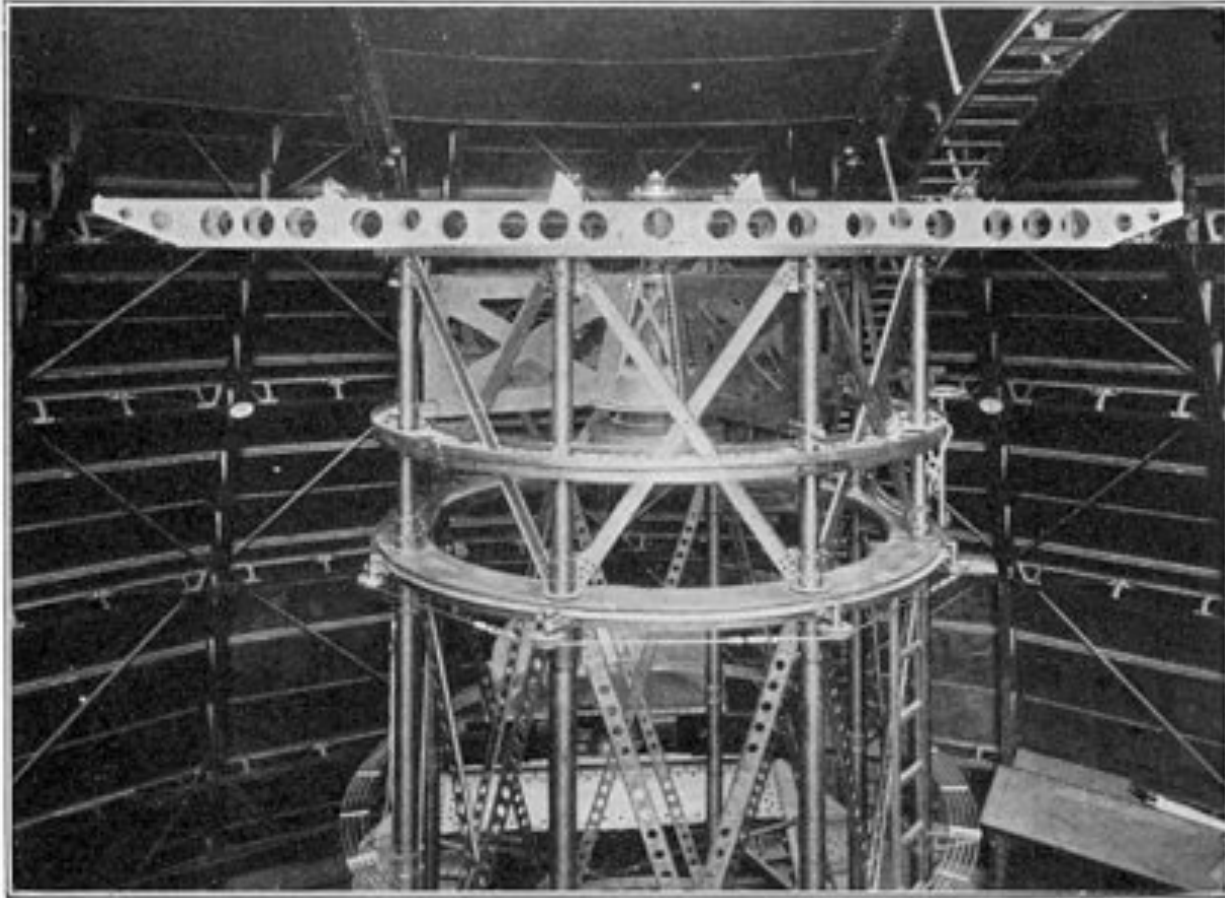
Radio source Cygnus A imaged at 6cm



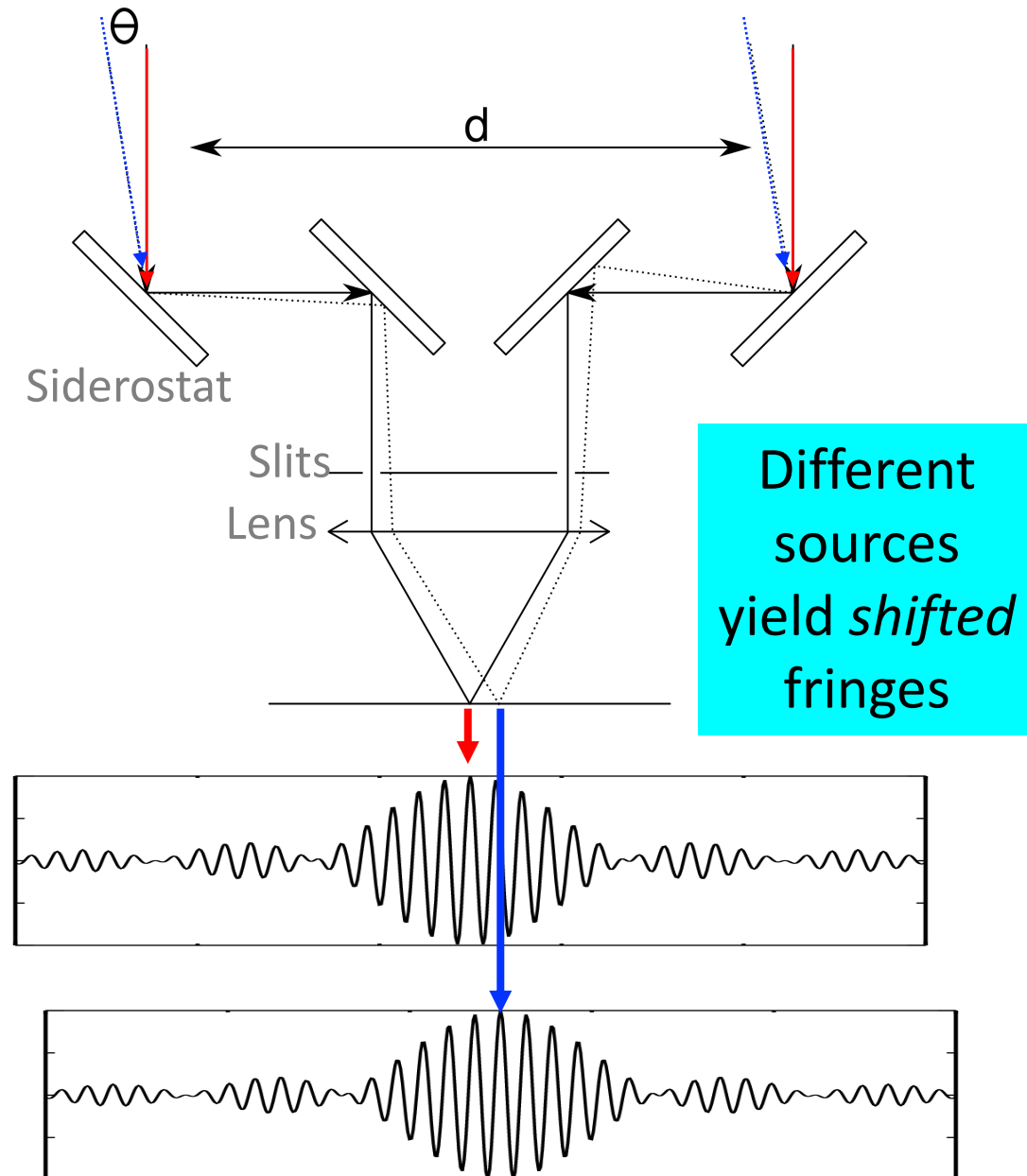
Center of M87 imaged at 1.3mm

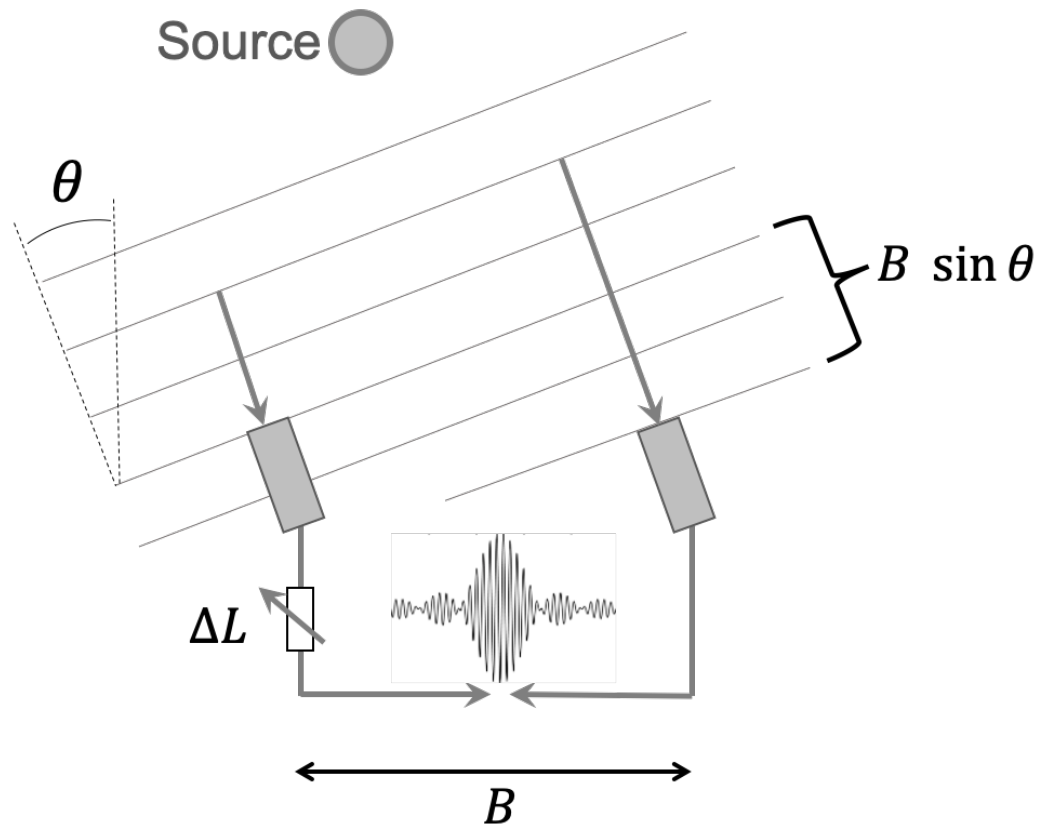
Single-photon techniques (classical)

In classical times



Michelson Stellar Interferometer at Mt. Wilson c. 1920, after original idea by Michelson & Fizeau c. 1890

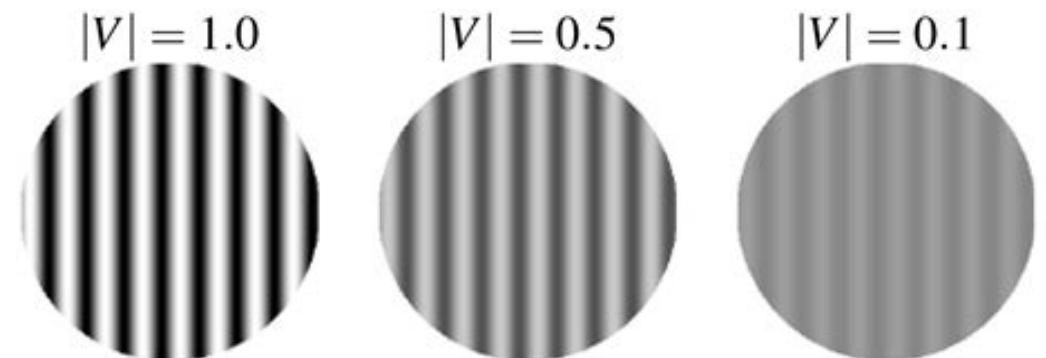
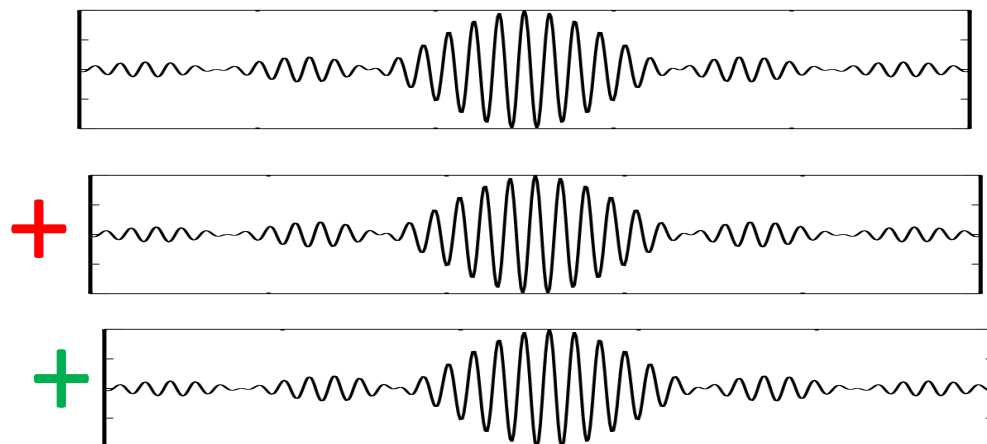


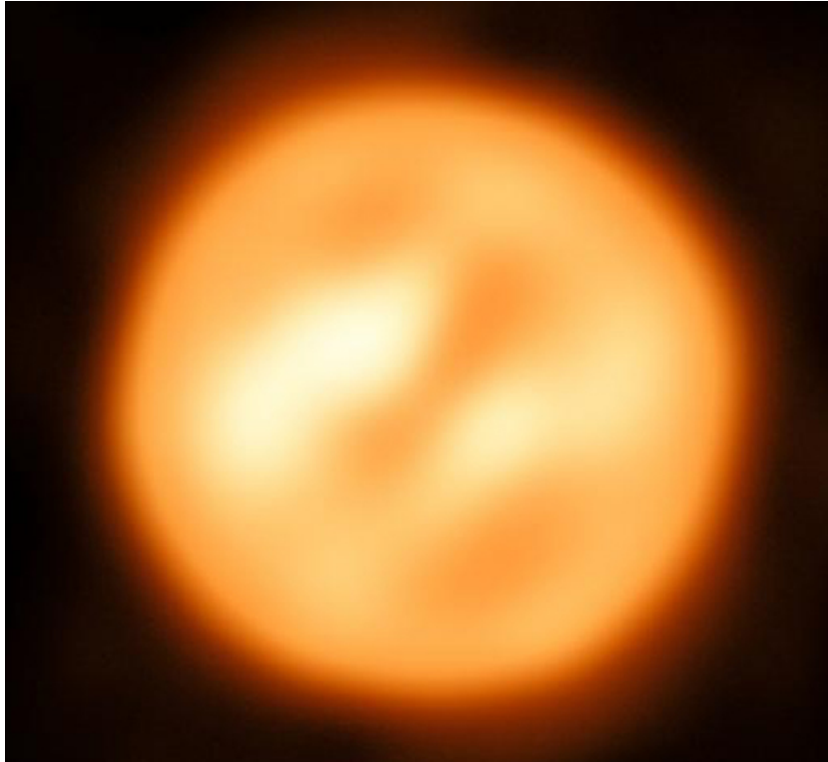


Each source i at sky position θ_i produces a fringe shifted by phase amount $\Delta\phi = 2\pi B \sin \theta_i / \lambda$

Intensity pattern is sum over all sources \rightarrow Fourier moment!

Fringe contrast(/visibility) measures amplitude of Fourier moment at wavenumber $k \approx 2\pi B / \lambda$





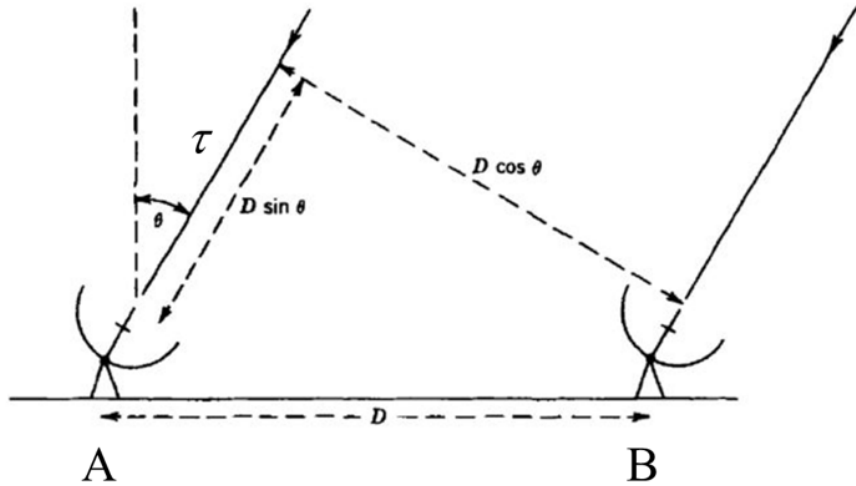
Dynamic convection on Antares
(VLTI, ESO)

Each fringe observation measures
amplitude and *phase* of Fourier
moment along baseline vector at
specific wavenumber.

Repeat for many different
baselines/wavenumbers and invert to
reconstruct original image.
(Note Earth rotation synthesis)

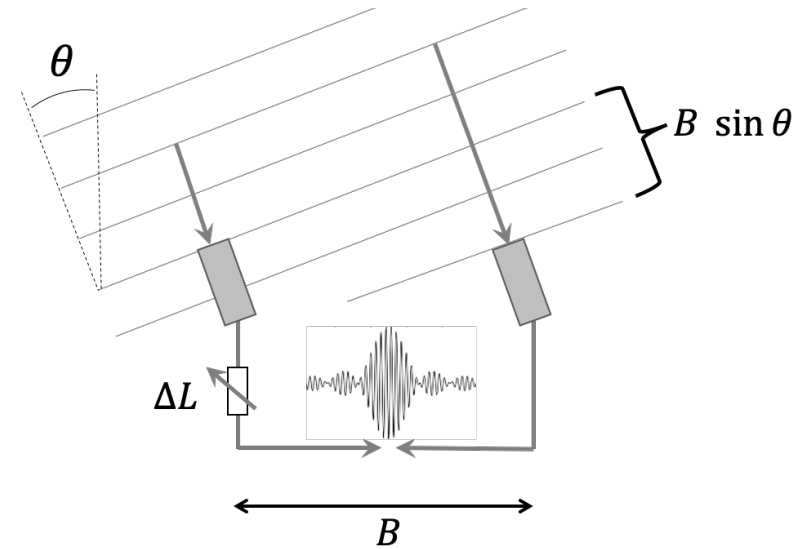
Measurement at baseline B
sensitive to source features
with angular size $\Delta\theta \sim \lambda/B$

Radio $\bar{n} \gg 1$



Can literally record entire waveform, over some band, separately at each receiver station and **interfere later offline**

$\bar{n} \ll 1$ Optical



One photon at a time! Need to bring paths to common point **in real time**

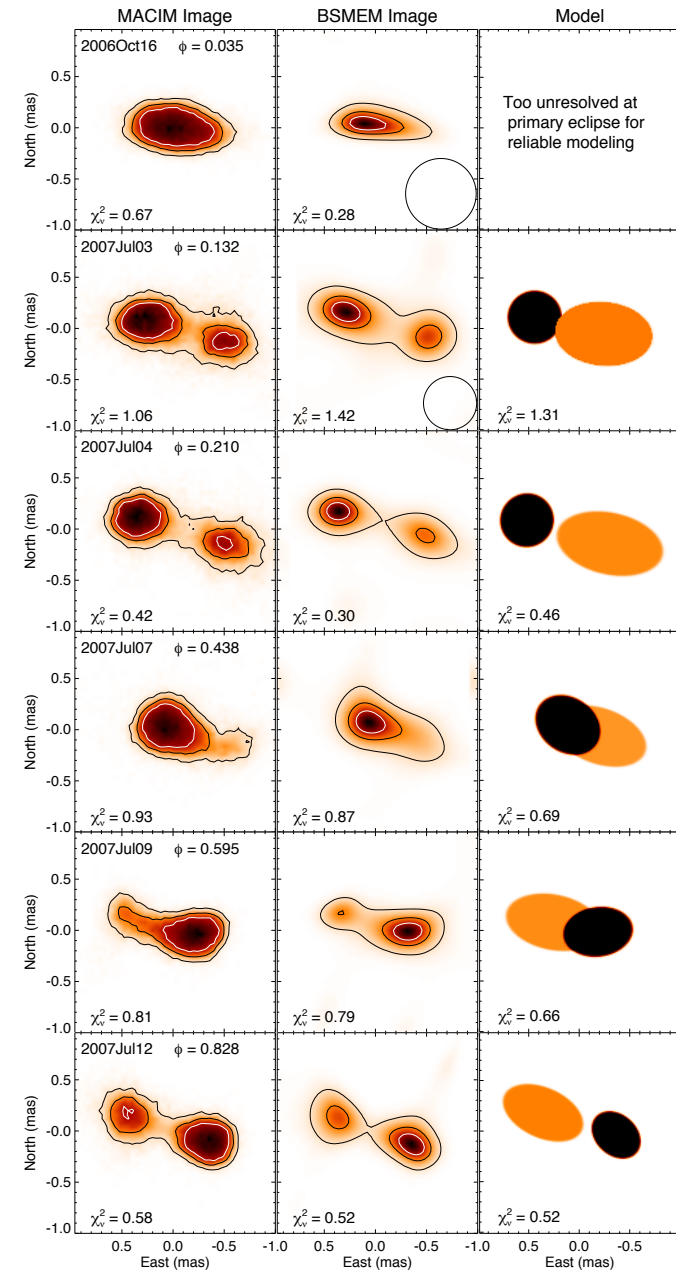
Need path length *compensated* to better than $c/\text{bandwidth}$

Need path length *stabilized* to better than λ

How cool is this?



CHARA Collaboration, “First Resolved Images of the Eclipsing and Interacting Binary β Lyrae”; arXiv:0808.0932, The Astrophysical Journal, 684: L95–L98, 2008 September 10



Classical summary

All very well-known at Caltech/JPL! Owens Valley, Keck, etc.

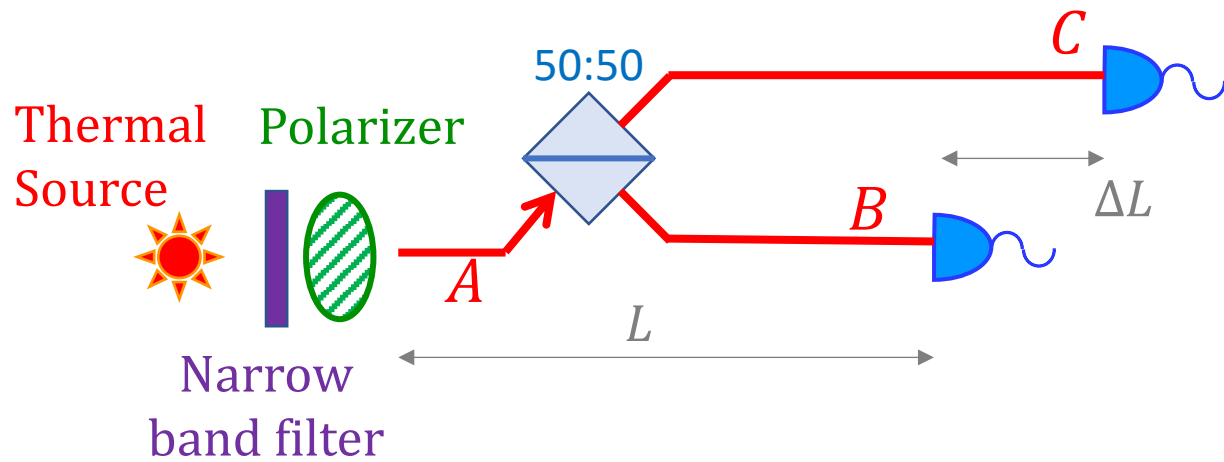
- EM waves interfere with themselves; single photons do same
- Interferometer sensitive to features on angular scale $\Delta\theta \sim \frac{\lambda}{B}$
- Drawbacks in ***optical***:
 - Need live optical link between stations
 - Need path length control precision on order $\lambda^2/\Delta\lambda$
 - Atmospheric effects enter at $O(1)$
 - Need to control polarization during transport
 - Practical limit on baselines $\sim 100\text{m}$

Two-photon techniques (quantum mechanical)

Prelude: Two-photon Intensity Interferometry

The curious HBT effect

“The birth of quantum optics”



Glauber theory of photodetection, c. 1963

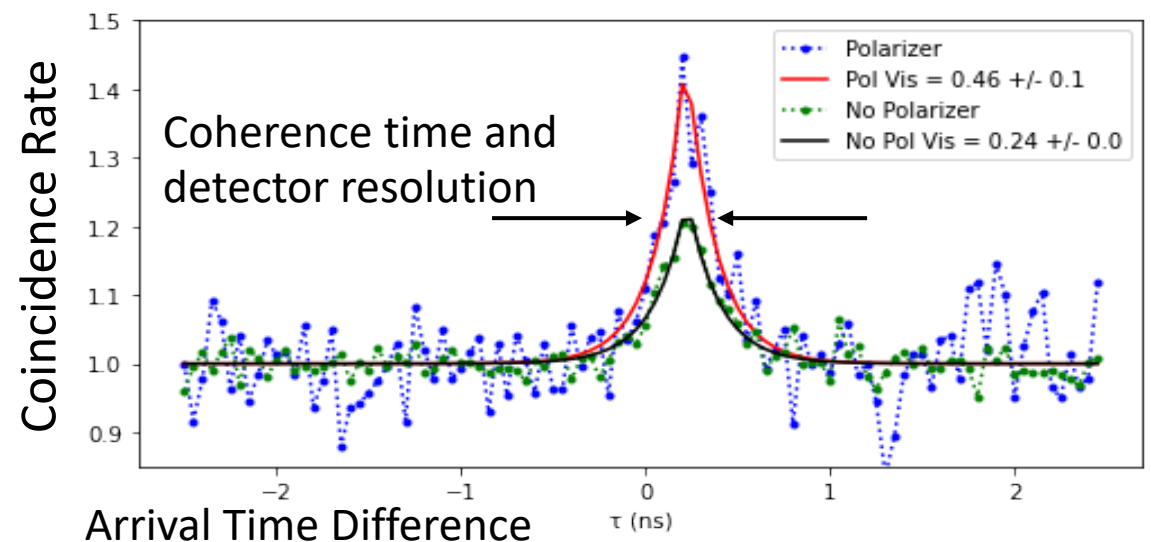
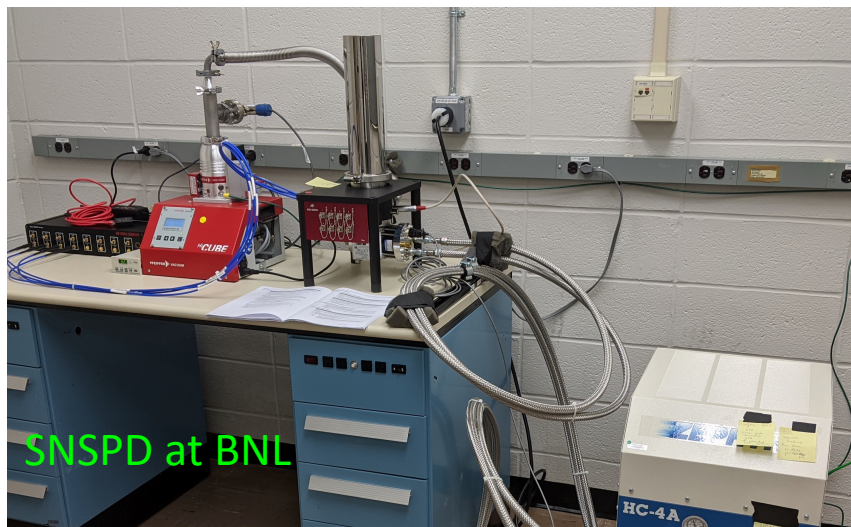
$$\text{Rate}^{BC}(t_B, t_C) \propto \|\hat{a}_B(t_B) \hat{a}_C(t_C) |\Psi\rangle\|^2$$

$$\propto \|\hat{a}_A(t_B - L/v) \hat{a}_A(t_C - (L + \Delta L)/v) |\Psi\rangle\|^2$$

$$\text{If } (t_B - L/v) = (t_C - (L + \Delta L)/v) = t_A$$

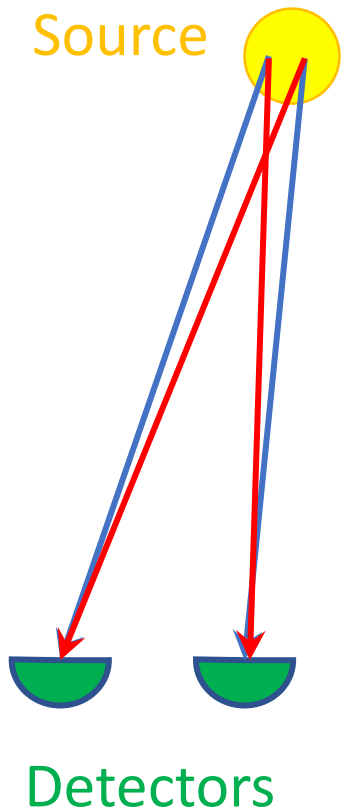
$$\text{then } \text{Rate}^{BC}(t_B, t_C) \propto \|\hat{a}_A(t_A)^2 |\Psi_{Th}\rangle\|^2$$

$$\|\hat{a}_A(t_A)^2 |\Psi_{Th}\rangle\|^2 = 2 \|\hat{a}_A(t_A) \hat{a}_A(t_A') |\Psi_{Th}\rangle\|^2$$



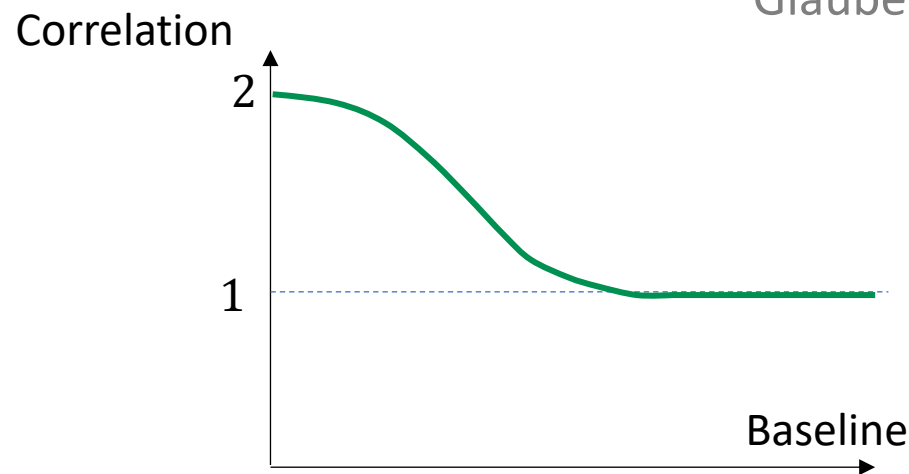
HBT and stellar sizes

In Hanbury Brown & Twiss (HBT) **intensity interferometry**, the observable is the *correlation* between photon detections at two separate detectors



$$\frac{(Pairs)}{(Singles)(Singles)} = \frac{\|\hat{a}_{\vec{k}1}\hat{a}_{\vec{k}2}|\Psi\rangle\|^2}{\|\hat{a}_{\vec{k}1}|\Psi\rangle\|^2 \|\hat{a}_{\vec{k}2}|\Psi\rangle\|^2} = \begin{cases} 1 & \vec{k}1 \neq \vec{k}2 \\ 2 & \vec{k}1 = \vec{k}2 \end{cases}$$

Glauber theory of photodetection, c. 1963



(It works for other bosons, too.)

High ride of HBT, 1956-1974 ...and beyond?



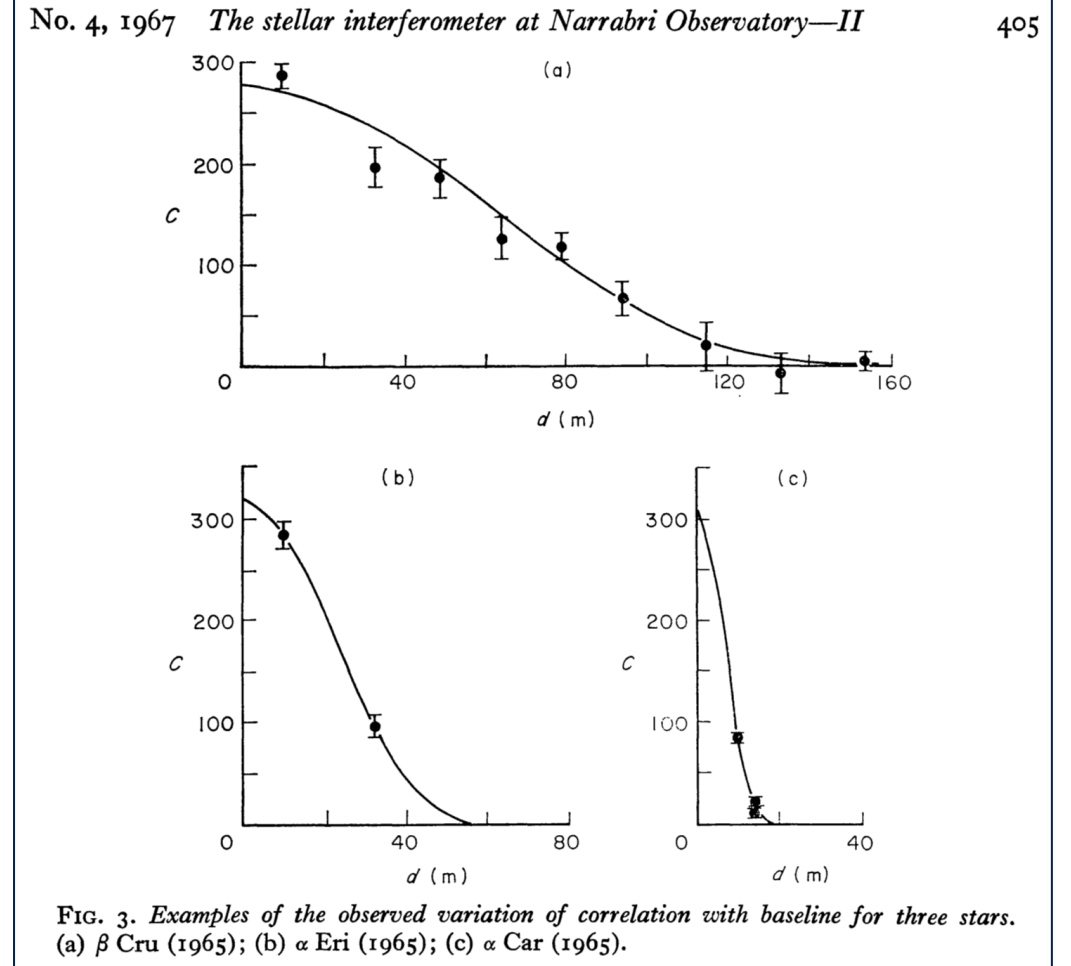
arXiv.org > astro-ph > arXiv:1810.08023

Astrophysics > Instrumentation and Methods for Astrophysics

Intensity Interferometry revival on the Côte d'Azur

Olivier Lai, William Guerin, Farrokh Vakili, Robin Kaiser, Jean Pierre Rivet, Mathilde Fouché, Guillaume Labeyrie, Etienne Samain, David Vernet

(Submitted on 18 Oct 2018)



HBT track record

- Advantages:
 - Separate stations with only classical connection
 - Arbitrary baselines, set by desired angular scale
 - No path-length corrections needed
 - Immune to atmospheric effects (at leading order)
- Drawbacks:
 - Low rates! Need to see coincident photon pairs, only pairs with $\Delta\nu \Delta t < 1$ will show effect; but more & finer spectral bins will help
 - Sensitive to *square* of image Fourier moment, washes out fine details
 - Used (thus far) mainly for gross features of bright objects

Two-photon techniques (quantum mechanical)

New: Two-Photon Amplitude Interferometry

Improved single photon interference?

PRL 109, 070503 (2012)

PHYSICAL REVIEW LETTERS

week ending
17 AUGUST 2012



Longer-Baseline Telescopes Using Quantum Repeaters

Daniel Gottesman*

Perimeter Institute for Theoretical Physics, Waterloo, Ontario, Canada

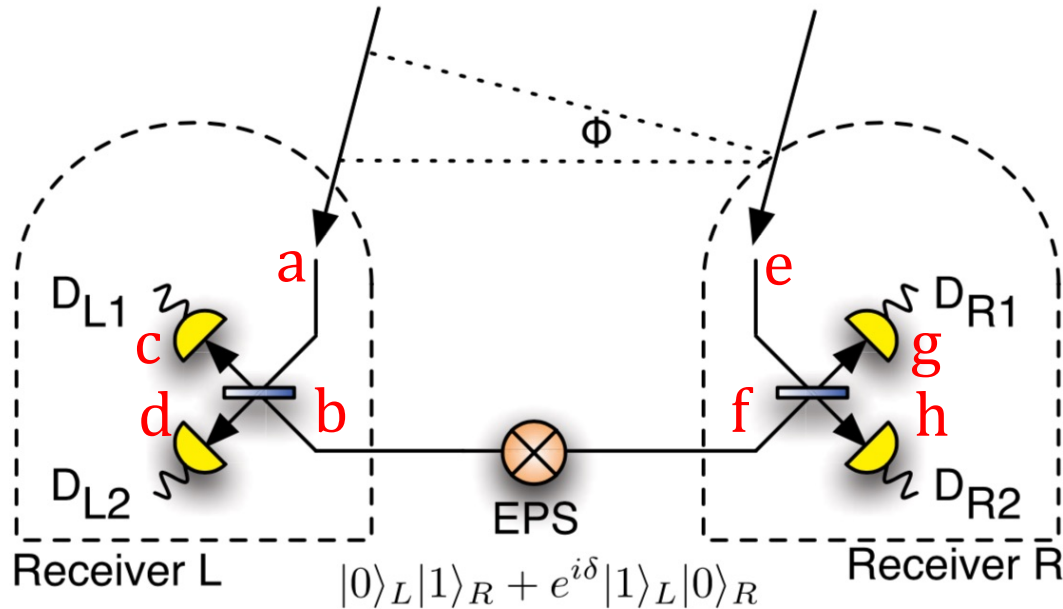
Thomas Jennewein†

Institute for Quantum Computing, University of Waterloo, Waterloo, Ontario, Canada

Sarah Croke‡

Perimeter Institute for Theoretical Physics, Waterloo, Ontario, Canada

(Received 25 October 2011; revised manuscript received 22 May 2012; published 16 August 2012)



$$\Psi^{\text{Initial}} = \psi_1\psi_2 = \frac{1}{2} \underbrace{(\hat{a}^\dagger + e^{i\delta_1} \hat{e}^\dagger)}_{\text{Sky photon}} \underbrace{(\hat{b}^\dagger + e^{i\delta_2} \hat{f}^\dagger)}_{\text{Ground photon}}$$

Sky photon Ground photon

Beam
Splitters

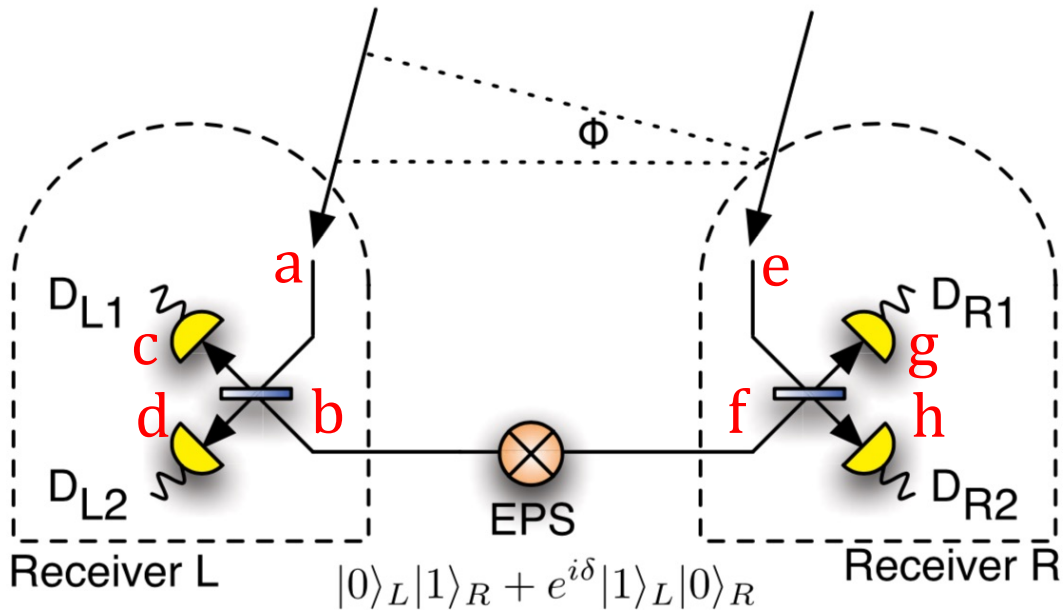
$$\begin{aligned} \hat{a}^\dagger &\rightarrow (\hat{c}^\dagger + \hat{d}^\dagger)/\sqrt{2} & \hat{b}^\dagger &\rightarrow (\hat{c}^\dagger - \hat{d}^\dagger)/\sqrt{2} \\ \hat{e}^\dagger &\rightarrow (\hat{g}^\dagger + \hat{h}^\dagger)/\sqrt{2} & \hat{f}^\dagger &\rightarrow (\hat{g}^\dagger - \hat{h}^\dagger)/\sqrt{2} \end{aligned}$$

$$\Psi^{\text{Output}} = (1/4)(\hat{c}^\dagger\hat{c}^\dagger - \hat{d}^\dagger\hat{d}^\dagger + e^{i(\delta_1+\delta_2)}(\hat{g}^\dagger\hat{g}^\dagger - \hat{h}^\dagger\hat{h}^\dagger) + (e^{i\delta_1} + e^{i\delta_2})(\hat{c}^\dagger\hat{g}^\dagger - \hat{d}^\dagger\hat{h}^\dagger) + (e^{i\delta_1} - e^{i\delta_2})(\hat{c}^\dagger\hat{h}^\dagger + \hat{d}^\dagger\hat{g}^\dagger))$$

$$\begin{aligned} P(c^2) = P(d^2) = P(g^2) = P(h^2) &= 1/8 \\ P(cg) = P(dh) &= (1/8)(1 + \cos(\delta_1 - \delta_2)) \\ P(ch) = P(dg) &= (1/8)(1 - \cos(\delta_1 - \delta_2)) \end{aligned}$$

Two-photon amplitude interferometry

$$\frac{N(cg) + N(dh) - (N(ch) + N(dg))}{N(cg) + N(dh) + N(ch) + N(dg)}$$



New visibility observable:

$$\frac{N(cg) + N(dh) - (N(ch) + N(dg))}{N(cg) + N(dh) + N(ch) + N(dg)}$$

$$= \cos(\delta_1 - \delta_2)$$

$$= \cos\left(\frac{2\pi \sin \theta b}{\lambda} - \delta_{\text{Ground}}\right)$$

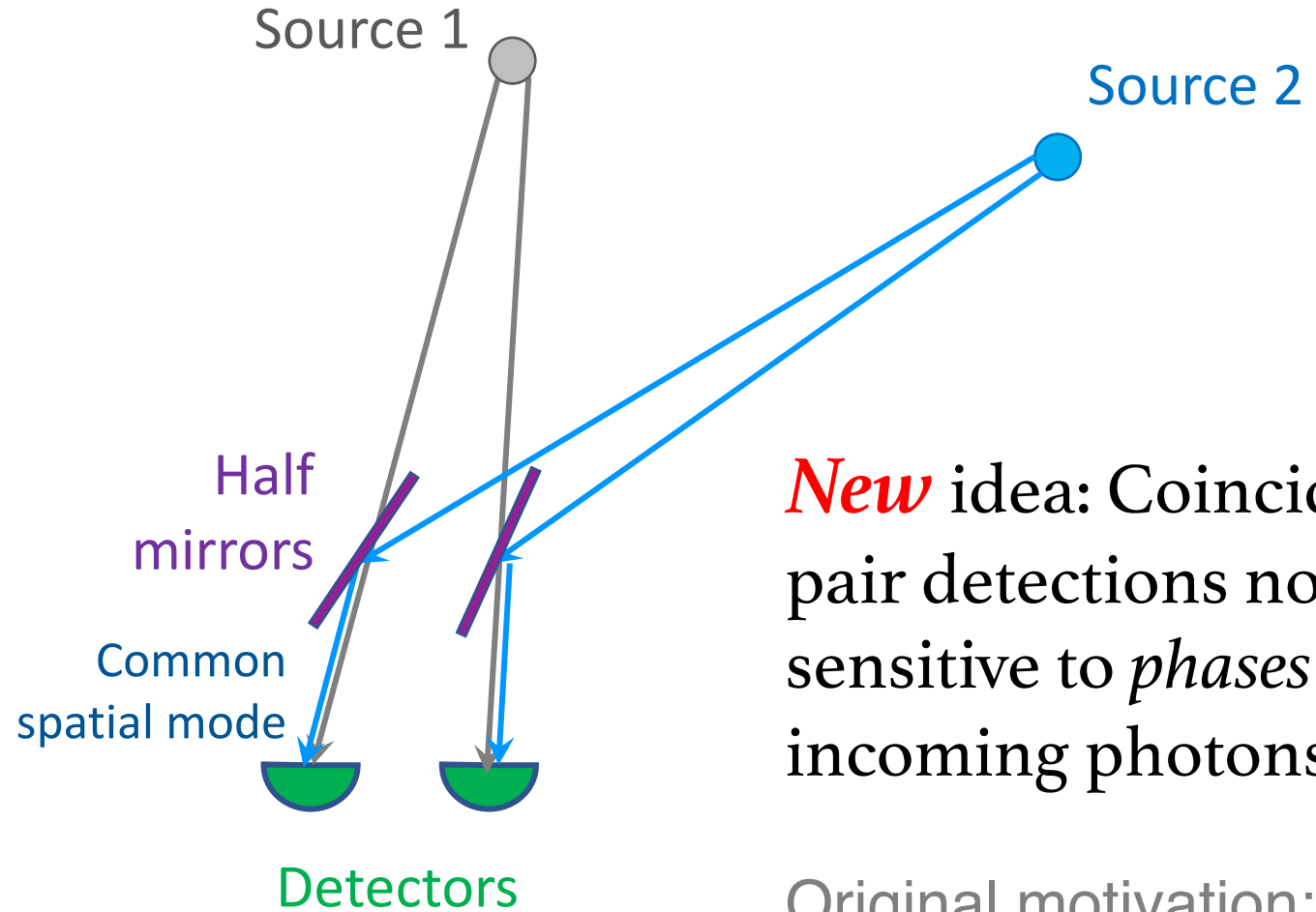
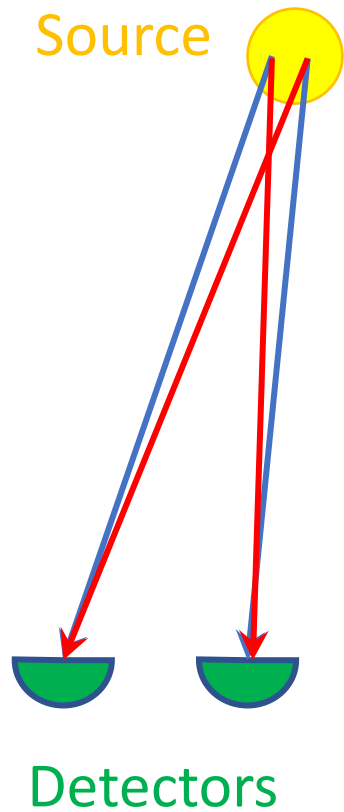
- Same measurement as single-photon interferometry, if ground photons are available
- Can be interpreted as *quantum teleportation* of sky photon from one station to the other

Two-photon spin-off technique

New: Two-Photon Amplitude Interferometry for *Astrometry**

* Astrometry = measurement of *positions* of objects on the sky

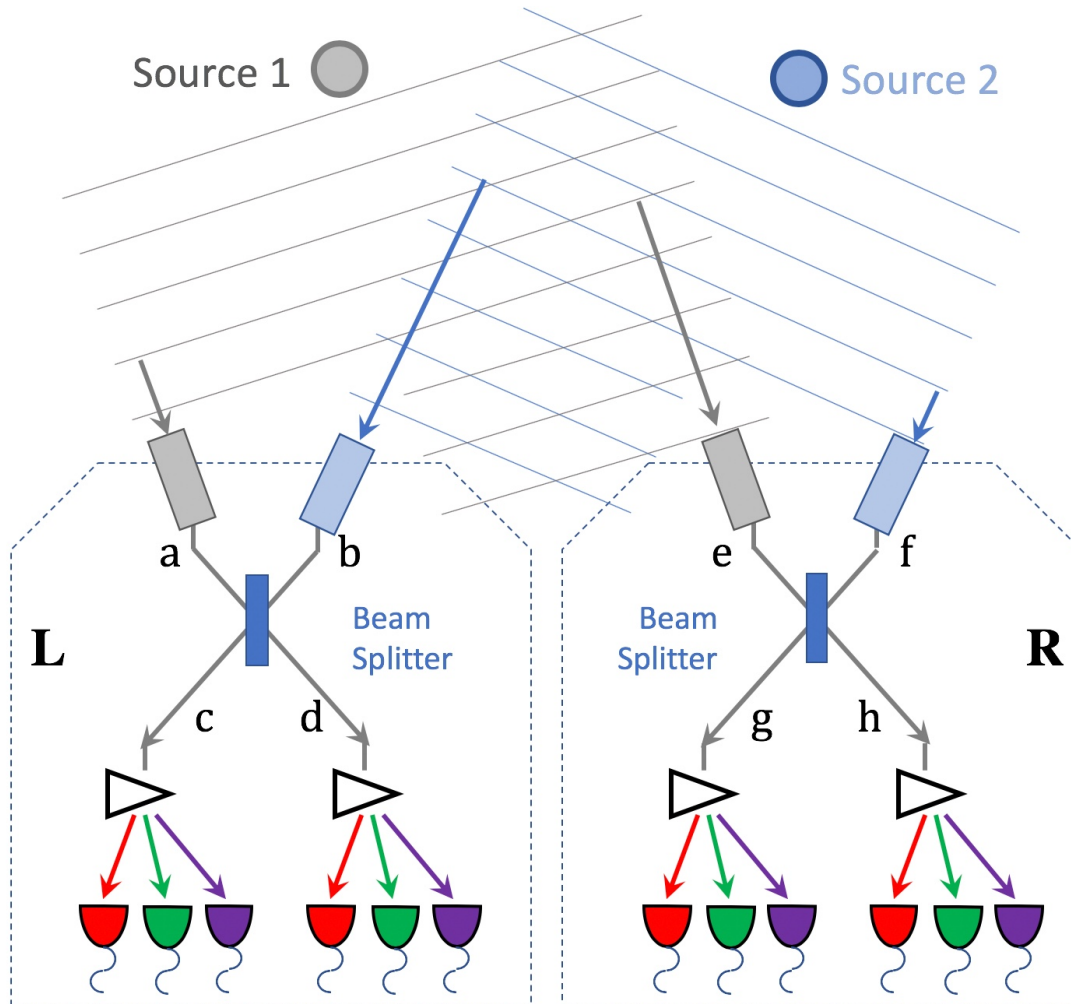
HBT with two sources?



New idea: Coincident pair detections now sensitive to *phases* of incoming photons

Original motivation: gravitational waves

Idea: two photons from two sky sources



arXiv.org > astro-ph > arXiv:2010.09100

Astrophysics > Instrumentation and Methods for Astrophysics

[Submitted on 18 Oct 2020 (v1), last revised 4 Nov 2020 (this version, v2)]

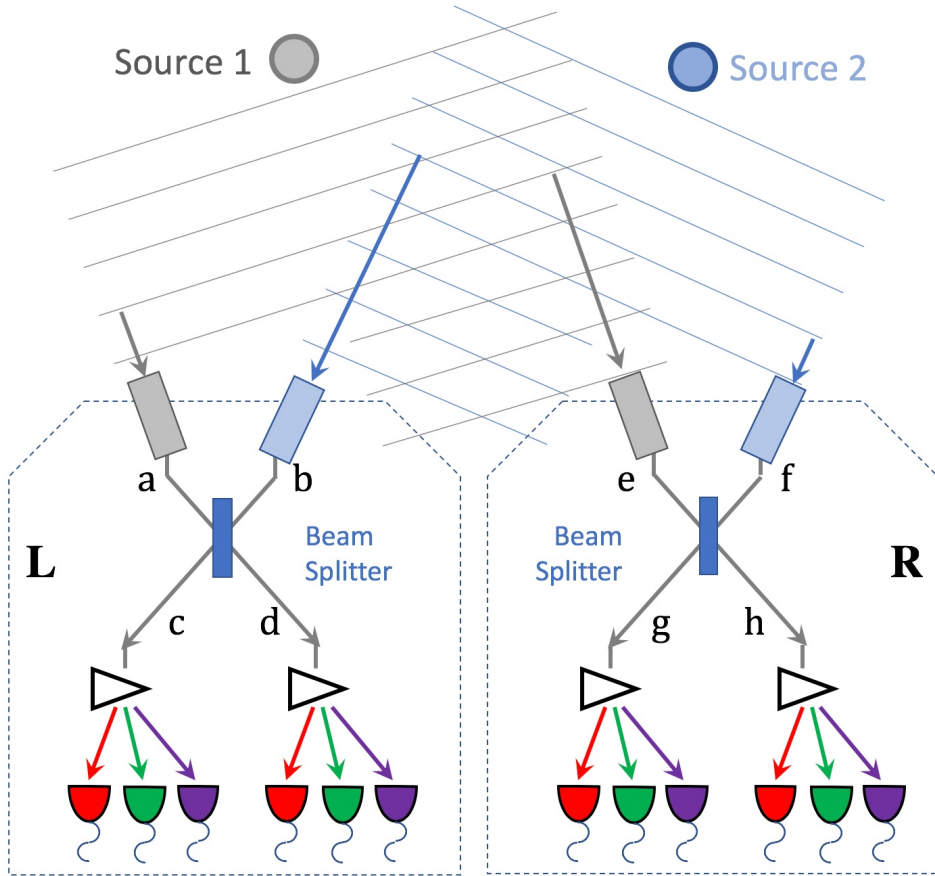
Two-photon amplitude interferometry for precision astrometry

Paul Stankus, Andrei Nomerotski, Anže Slosar, Stephen Vintskevich

Topology is equivalent to GJC(2012) but now with both photons from the sky, and from different objects

Sensitive to *difference* in path length differences  opening angle!

Does *not* require live optical link between stations; can use arbitrary baseline



Observable is the number/rate of coincidences $xy = \{cg, dh\}$ or $\{ch, dg\}$ at different stations.

(Can do many spectral bins in parallel.)

Quantum mechanics (Fock state) version; quickie:

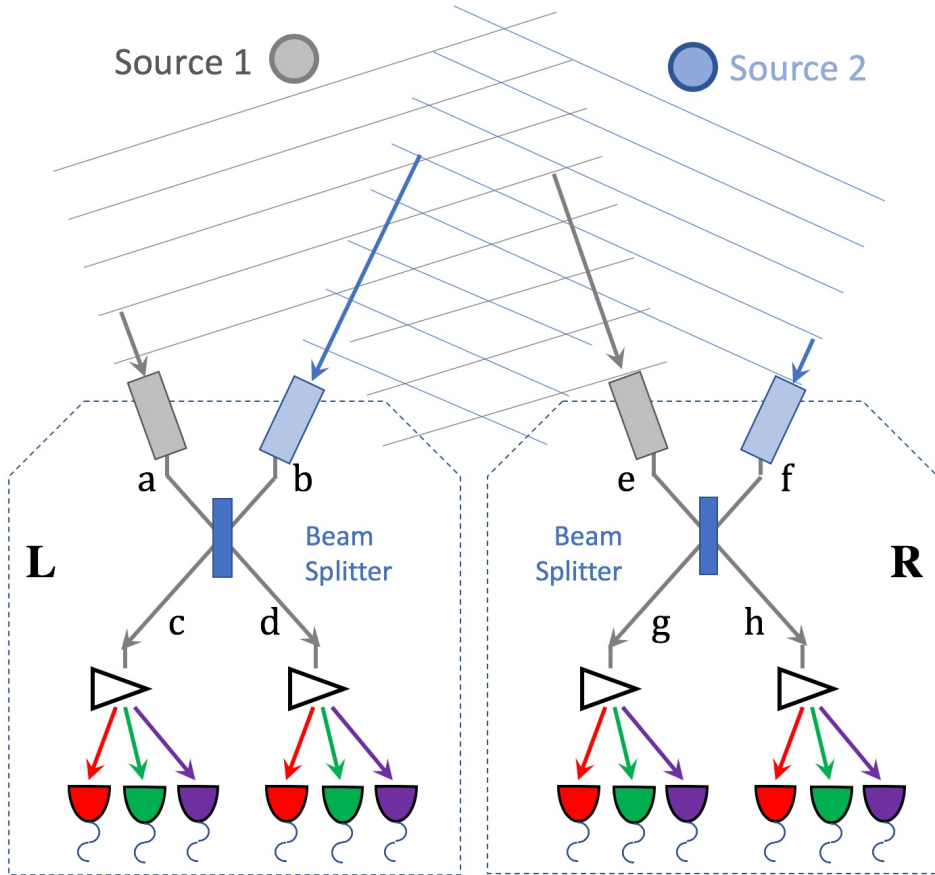
$$\langle N(xy) \rangle = \frac{k(S_1 + S_2)^2}{8} \left[1 \pm V_{2PS} \cos \left[\frac{2\pi B}{\lambda} (\sin \theta_1 - \sin \theta_2) + \frac{2\pi \Delta L}{\lambda} \right] \right]$$

Quantum field theory version; full:

$$N_c(xy) = \eta_1 \eta_2 A^2 \int_0^{T_r} P_{L,R,\tau}^{\text{two photons}} d\tau =$$

$$A^2 \eta_1 \eta_2 T_r \left[(I_1 + I_2)^2 + I_1^2 \frac{\tau_c g_{11}}{T_r} + I_2^2 \frac{\tau_c g_{22}}{T_r} \pm \right.$$

$$\left. 2I_1 I_2 \frac{\tau_c g_{12}}{T_r} \cos \left(\frac{\omega_0 B (\sin \theta_1 - \sin \theta_2)}{c} + \frac{\omega_0 \Delta L}{c} \right) \right]$$



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Annotations:

- Base combinatoric pair rate: points to $(I_1 + I_2)^2$
- HBT enhancement: points to $I_1^2 \frac{\tau_c g_{11}}{T_r} + I_2^2 \frac{\tau_c g_{22}}{T_r}$
- Oscillatory term (New!): points to the cosine term

Idea: Earth rotation fringe scan

$$\langle N(xy) \rangle = \frac{k(S_1 + S_2)^2}{8} \left[1 \pm V_{2\text{PS}} \cos \left[\frac{2\pi B}{\lambda} (\sin \theta_1 - \sin \theta_2) + \frac{2\pi \Delta L}{\lambda} \right] \right]$$

This will evolve as the Earth rotates

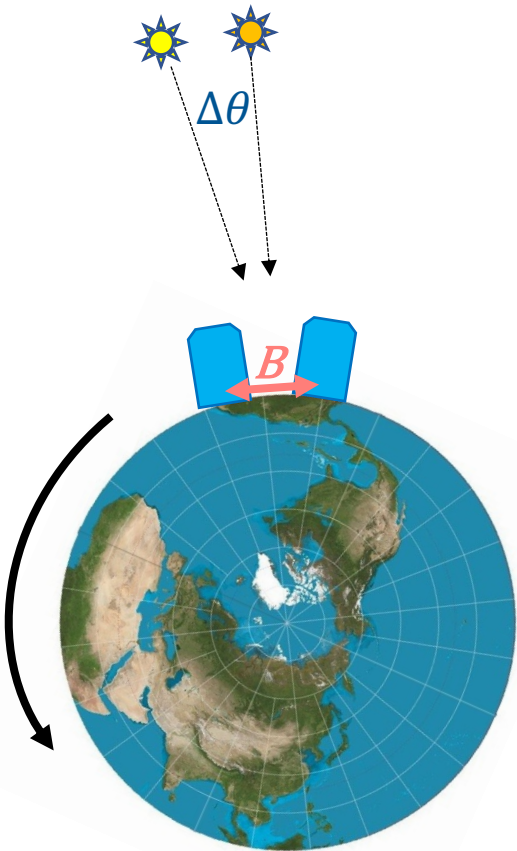
$$\langle N_{xy} \rangle(t) = \bar{N}_{xy} [1 \pm V \cos(\omega_f t + \Phi)]$$

Coincidence rates oscillate

$$\omega_f = \frac{2\pi B \Omega_{\oplus} \sin \theta_0}{\lambda} \Delta \theta$$

Fringe oscillation rate is a direct measure of sources' opening angle!

Can measure with high precision



World-competitive precision

$$\sigma [\Delta\theta] = \sqrt{\frac{6}{\pi^2 \kappa} \frac{1}{V} \frac{\lambda}{B} \frac{1}{T \Omega_{\oplus} \sin \theta_0} \frac{1}{\sqrt{\bar{n} T}}}$$

\bar{n} = average pair rate

T = total observation time

A modest experiment:

- Bright stars, mag 2
- 1 m² collecting area
- 10⁴ seconds observation
- 0.15 nsec time resolution
- 10⁴ spectral channels

Idea: Dynamic Astrometry

Track day-over-day changes in $\Delta\theta$ to observe parallax, proper motion, orbital motion, gravitational lensing

 $\sigma [\Delta\theta] \sim 10 \mu\text{as} (\sim 10^{-11} \text{ rad})$

1 mas **HIPPARCOS** (1989-1993)
7 μas **GAIA** (2013-)

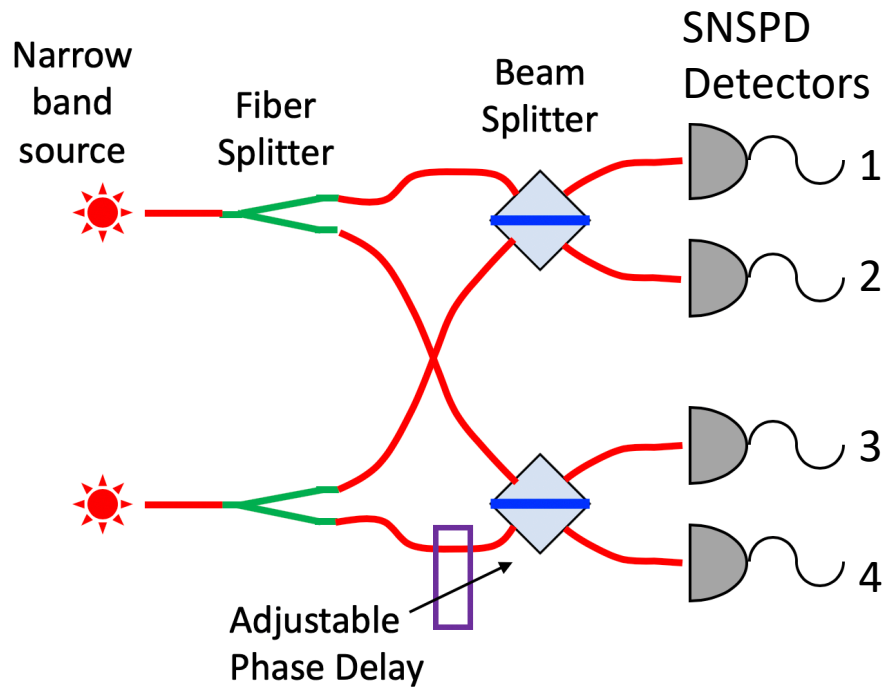
Astrophysics topics in dynamic astrometry

- Parallax: improved distance ladder
- **Proper motions:** local dark matter patterns
- **Microlensing,** see motions and shape changes
- **Gravitational waves** at mid-frequency
- **Quantum applications,** e.g. quantum key distribution

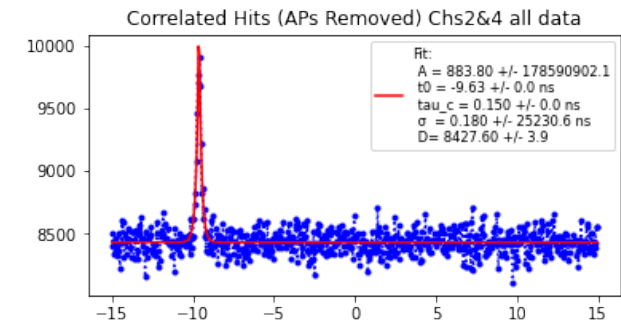
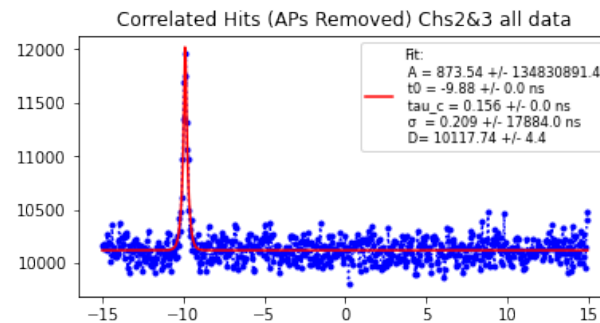
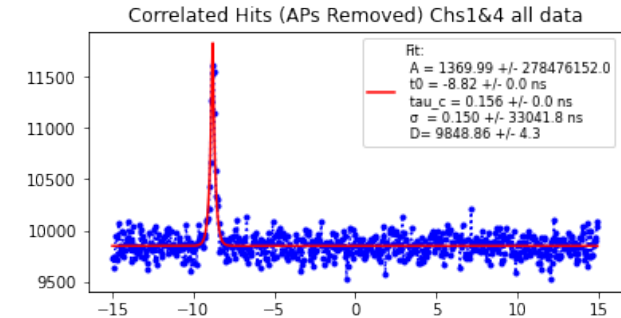
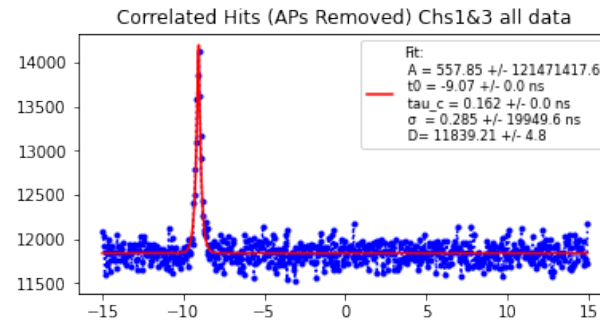
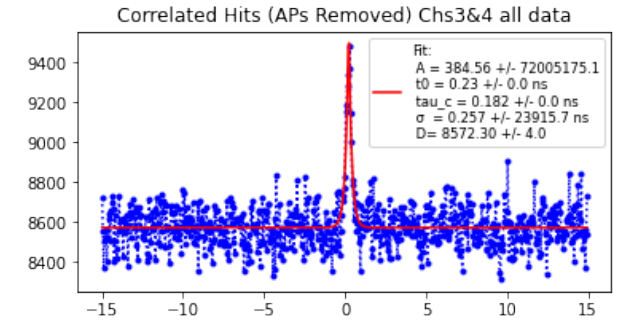
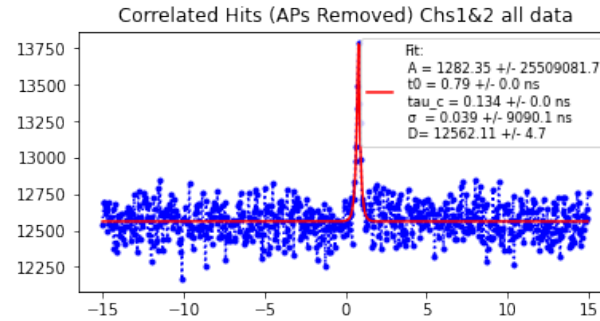
Further ideas are encouraged!

Experiments in progress

Supported at BNL by DOE HEP
QuantISED grant 2020-21



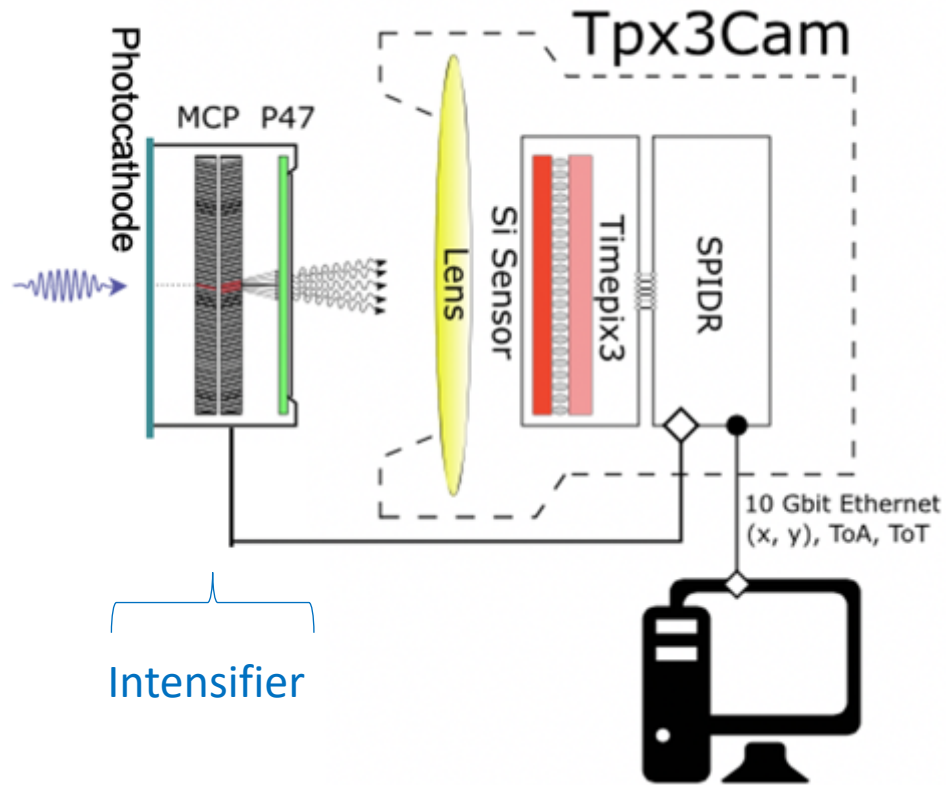
Check: We can see HBT coincidence enhancement peak in all channel combinations



Future detector requirements

- Two essential figures of merit:
 - Number of detectors/spectroscopic channels (more pairs)
 - Detector time resolution (wider spectroscopic bins, more pairs per detector)
- Fast pixel array (Timepix) + dispersive spectrograph (Echele?)
- Very fast single photon detectors – improved SNSPD?

Intensified camera is single photon sensitive



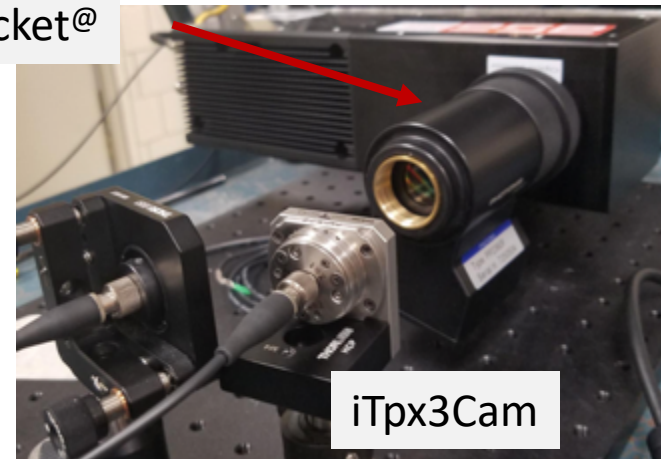
Quantum efficiency $\sim 30\%$

A.Nomerotski, Imaging and time stamping of photons with nanosecond resolution in Timepix based optical cameras, NIM A 937 (2019) 26



Image intensifier (Photonis PP0360EG)

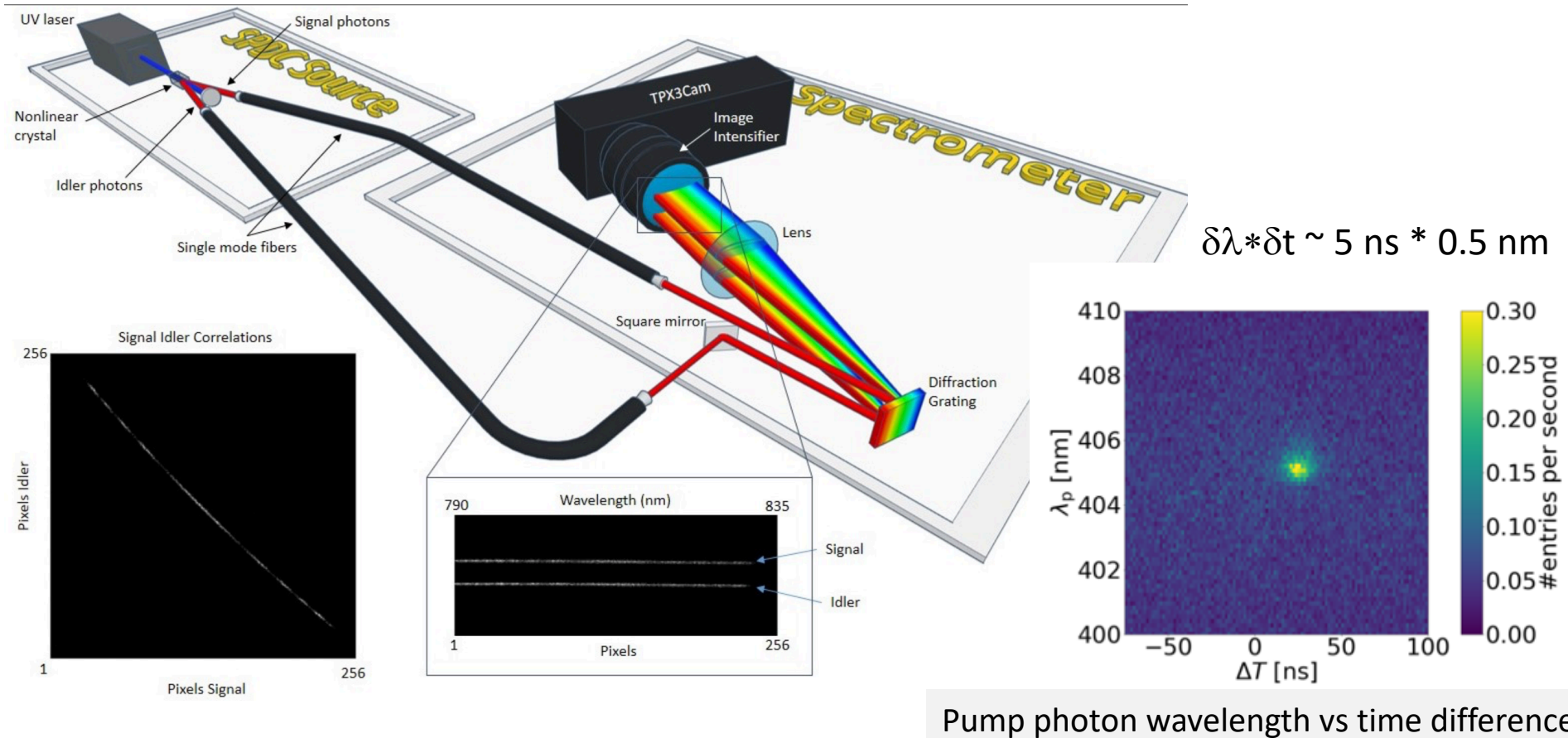
Cricket@



iTPx3Cam

Spectroscopic binning already demonstrated

In collaboration with NRC (Ottawa) D.England, Y.Zhang et al



Y Zhang, D England, A Nomerotski, P Svihra et al, Multidimensional quantum-enhanced target detection via spectrotemporal-correlation measurements, Physical Review A 101 (5), 053808

P Svihra et al, Multivariate Discrimination in Quantum Target Detection, Appl. Phys. Lett. **117**, 044001 (2020)

Just the beginning! A broad future program

- Observations with >2 receivers and >2 objects; phase closure?
- More complicated quantum states (GHZ, etc.)
- New kinds of entanglement distribution (polarization qubits, e.g.)
- Involvement of quantum memories to enhance pair rates; local expertise (SBU) with ^{87}Rb vapor room-temp QM's
- Atmospheric effect compensation
- On-sky experiments possible soon!

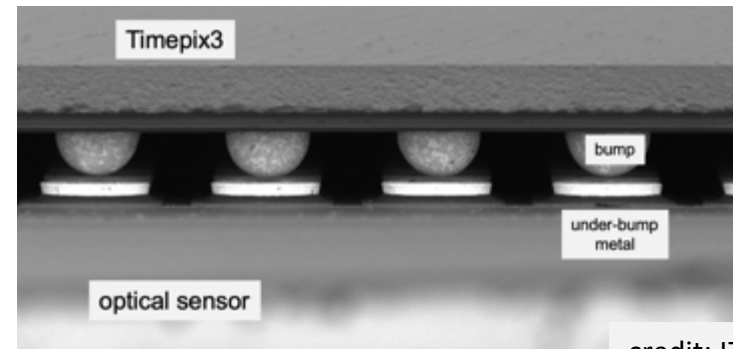
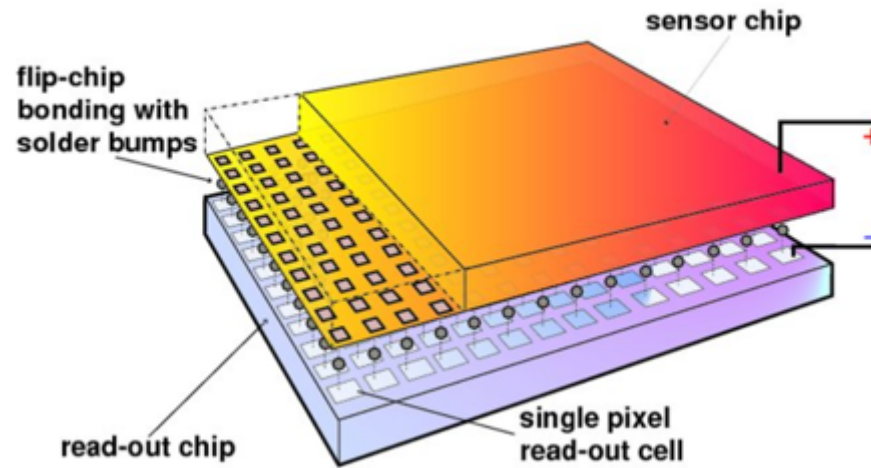
Points to take home

- Classical, single-photon interferometry reaches much higher resolutions, order milli-arcsec, than single telescopes; but practical issues limit maximum baselines
- Two-photon interferometry can permit independent stations over longer baselines; historical HBT is one example
- Two-photon techniques are in general quantum mechanical; new ideas suggest quantum technology can enhance interferometry
- One specific two-photon technique addresses dynamic astrometry, which will have interesting astrophysics applications
- There is a potentially broad program in quantum-assisted optical interferometry ahead

Backups

Hybrid pixel detectors

Have roots in R&D for LEP/LHC vertex detectors



credit: IZM

Lukas Tlustos and Erik H. M. Heijne, Performance and limitations of high granularity single photon processing X-ray imaging detectors, in CERN proceedings (2005)

- Decouple readout chip and sensor
- Optimize technologies for chip and sensor separately

Use different sensors with same readout, versatile approach for x-rays (Si, CZT)

→ we will use OPTICAL sensors

Timepix3 Camera → Tpx3Cam

Camera = sensor + ASIC + readout

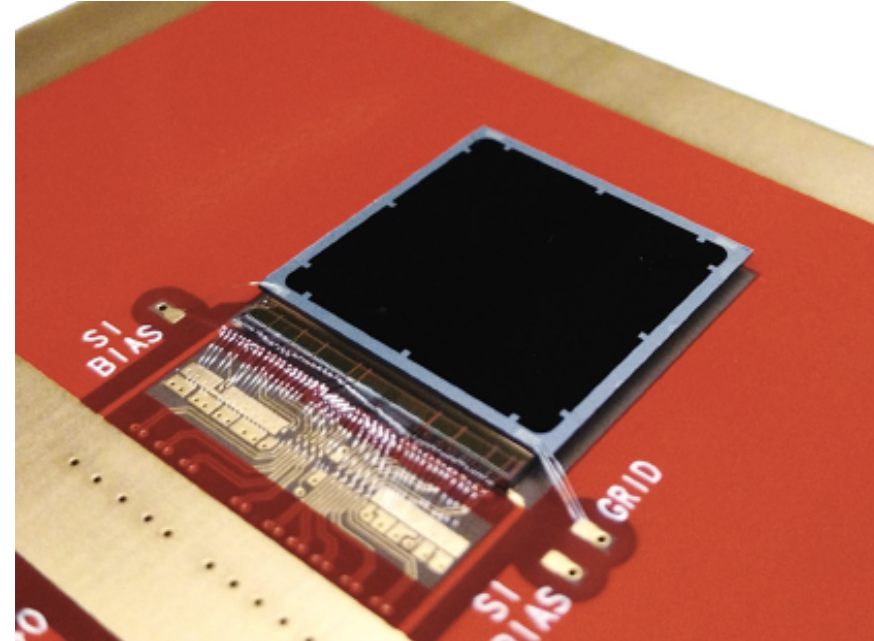
Optical sensor with high QE developed at BNL

- Sensor is bump-bonded to chip Timepix3

Timepix3 ASIC:

256 x 256 array, 55 x 55 micron pixel

- 1.56 ns timing resolution
- data-driven readout, 80 Mpix/sec, no deadtime



M. Fisher-Levine, A. Nomerotski, Timepixcam: a fast optical imager with time-stamping,
Journal of Instrumentation 11 (03) (2016) C03016.